

Mini-workshop on Global Trajectory Optimisation

ESTEC, 10th of September 2007

European Space Agency

Programme

10:00-10:10 **Opening** (Leopold Summerer , ESA-ACT)

10:10 - 11:00 **Global Trajectory Optimisation projects in the ACT** (Dario Izzo, Tamas Vinko and Claudio Bombardelli, ESA-ACT)

11:00 - 12:00 **Global Trajectory Optimisation: Can We Prune the Solution Space when Considering Deep Space Manoeuvres?** Ariadna Final Presentation, Politecnico di Milano and Michigan State University

12:00 - 13:00 **Global Trajectory Optimisation: Can We Prune the Solution Space when Considering Deep Space Manoeuvres?** Ariadna Final Presentation, Ecole des Mines de Paris

13:00 - 14:30 Lunch break

14:30 - 15:30 **Global Trajectory Optimisation: Can We Prune the Solution Space when Considering Deep Space Manoeuvres?** Ariadna Final Presentation, University of Glasgow and University of Reading

15:30 - 16:00 **An extension of GASP to DSM trajectories**, (Adam Zalcman, Jagiellonian University, Poland)

16:00 - 16:20 **ESOC plans on global trajectory optimisation** (Johannes Schoenmaekers, OPS-GFA)

16:20 - 17:00 Technical discussion and wrap-up

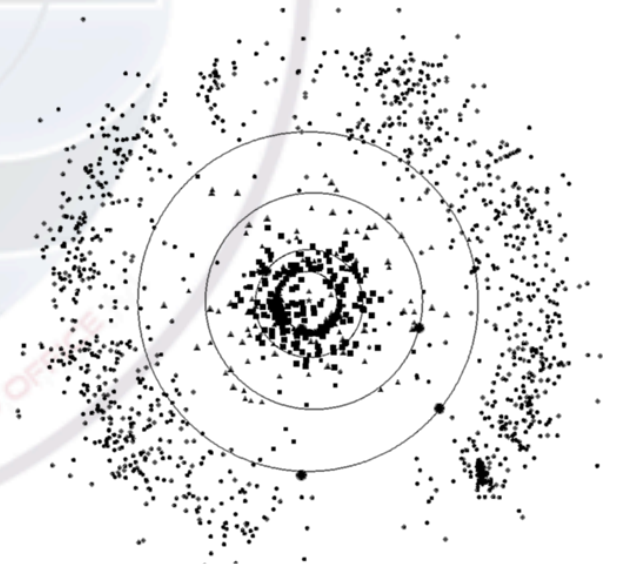
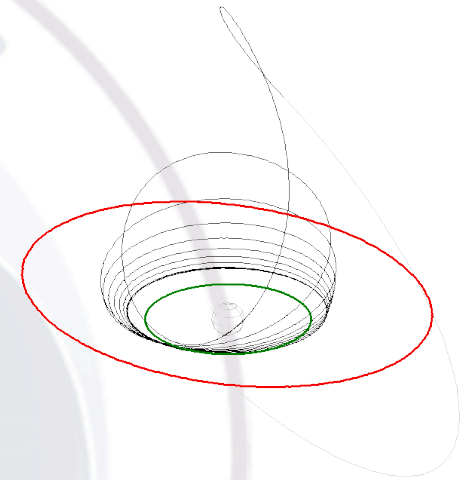
The increasing number of interplanetary missions that are proposed for the various ESA programs often requires a large number of trajectory/design options to be evaluated. At a preliminary stage this usually means the consideration of very large launch windows, different planetary fly-by sequences and of different design options. This small workshop wants to give an overview on different solutions that have been recently proposed by the spacecraft trajectory optimization community in response to the need of finding good preliminary solutions that may make the difference between a feasible and an unfeasible mission. The emphasis is put on global optimization

Interplanetary trajectories design

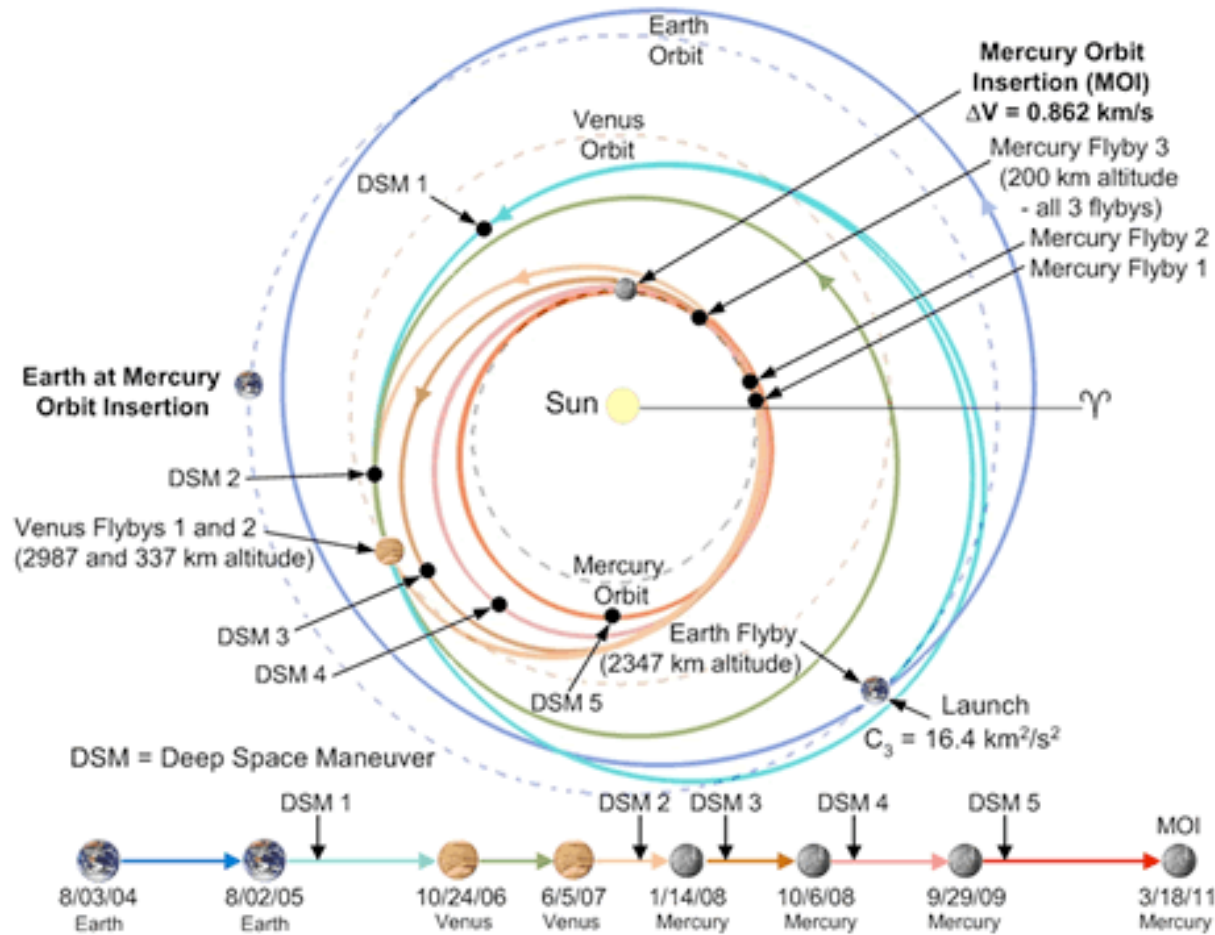
- An early step of any interplanetary space mission feasibility study
- Complex problem in its very mathematical nature:

$$\begin{aligned} \text{Minimise:} & \quad J(\mathbf{x}) \\ \text{Subject to:} & \quad \mathbf{g}(\mathbf{x}) \leq 0 \end{aligned}$$

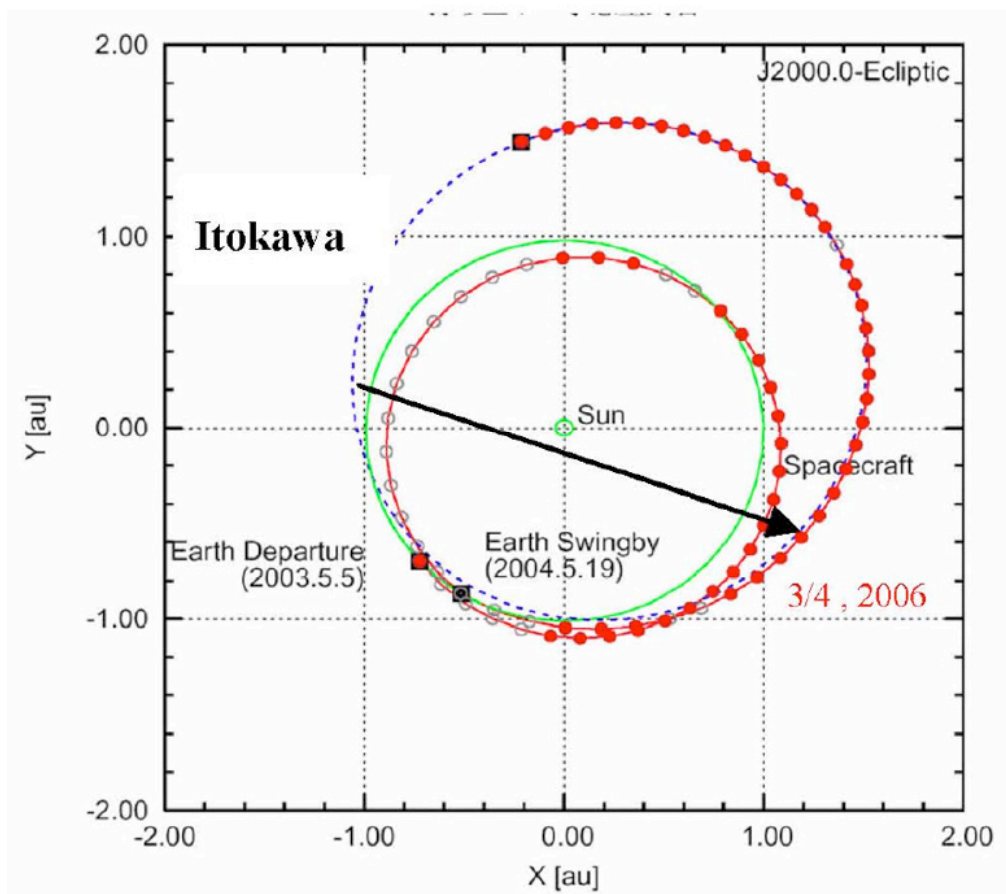
- There is more than meets the eye



Messenger

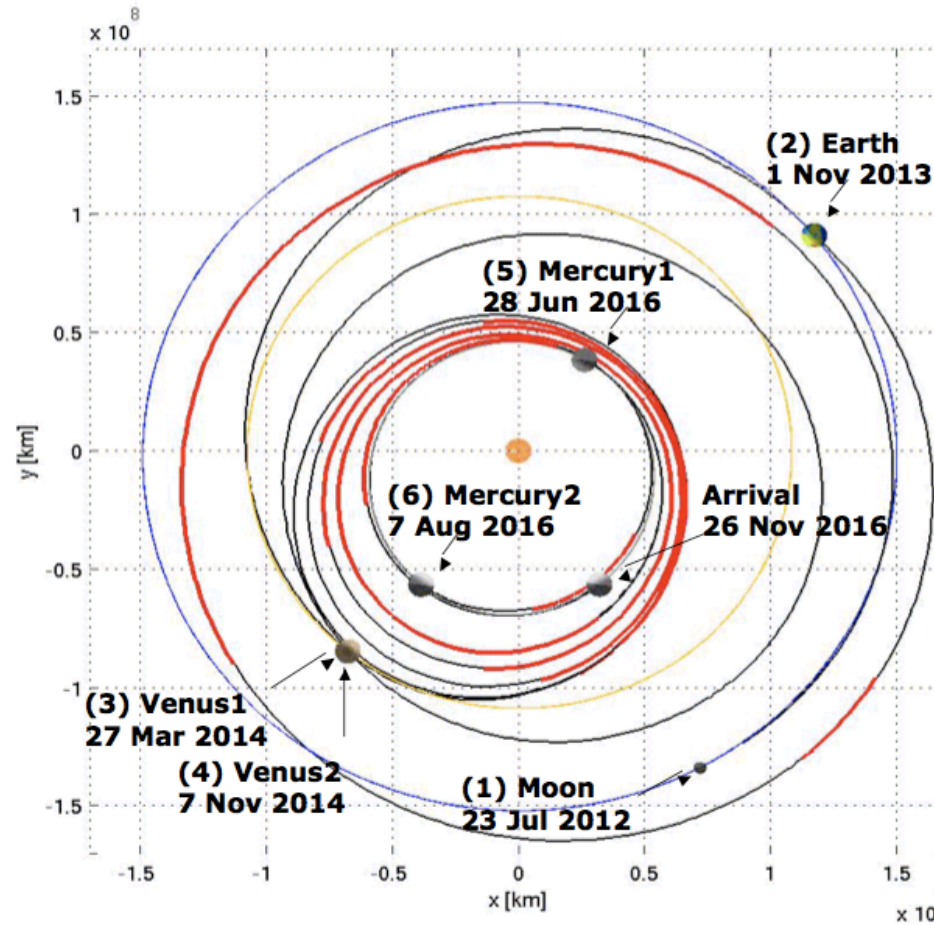


Hyabusa



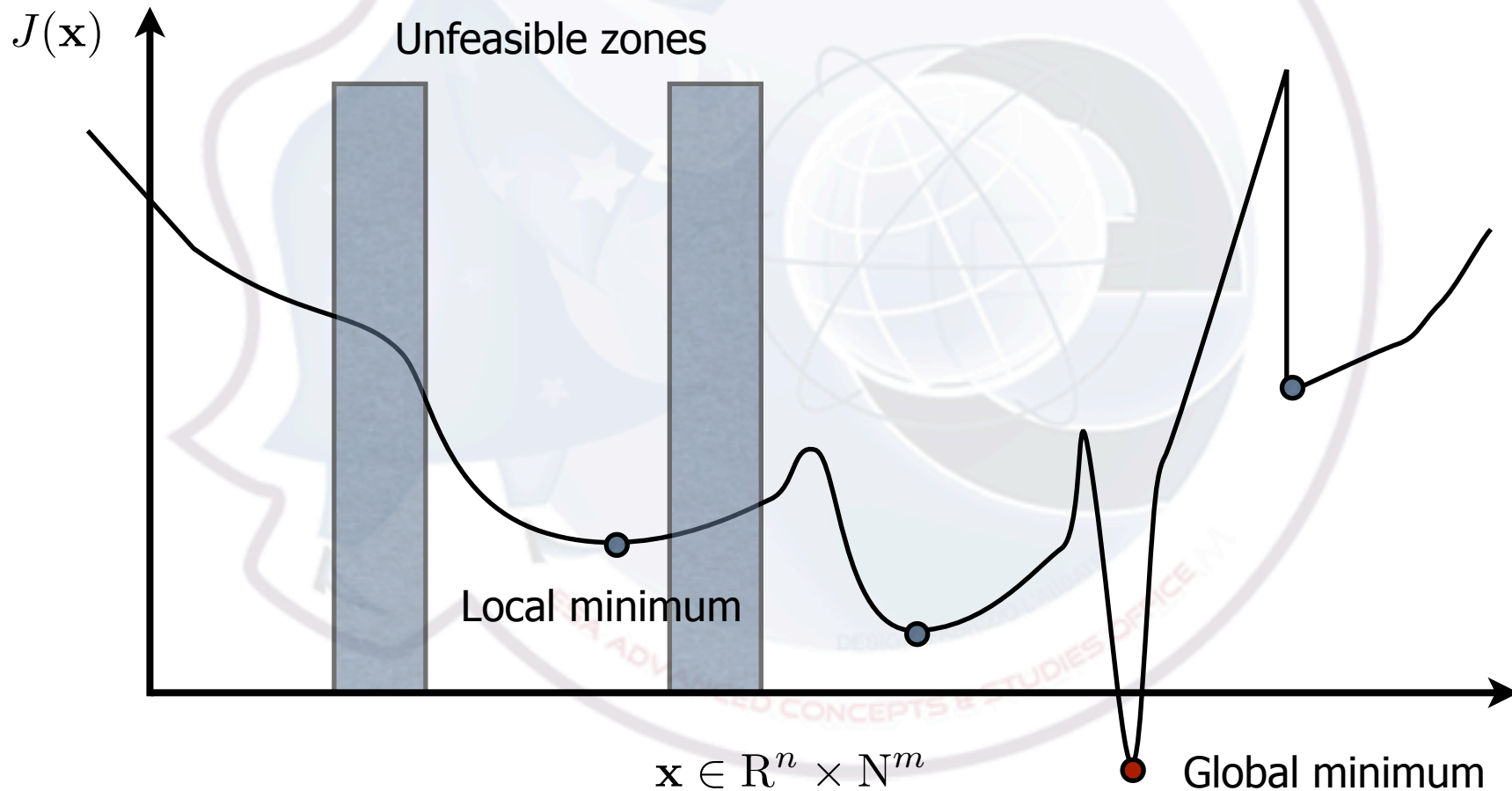


Bepi Colombo



Mathematical programming

$$\begin{aligned} \text{Minimise: } & J(\mathbf{x}) \\ \text{Subject to: } & \mathbf{g}(\mathbf{x}) \leq 0 \end{aligned}$$



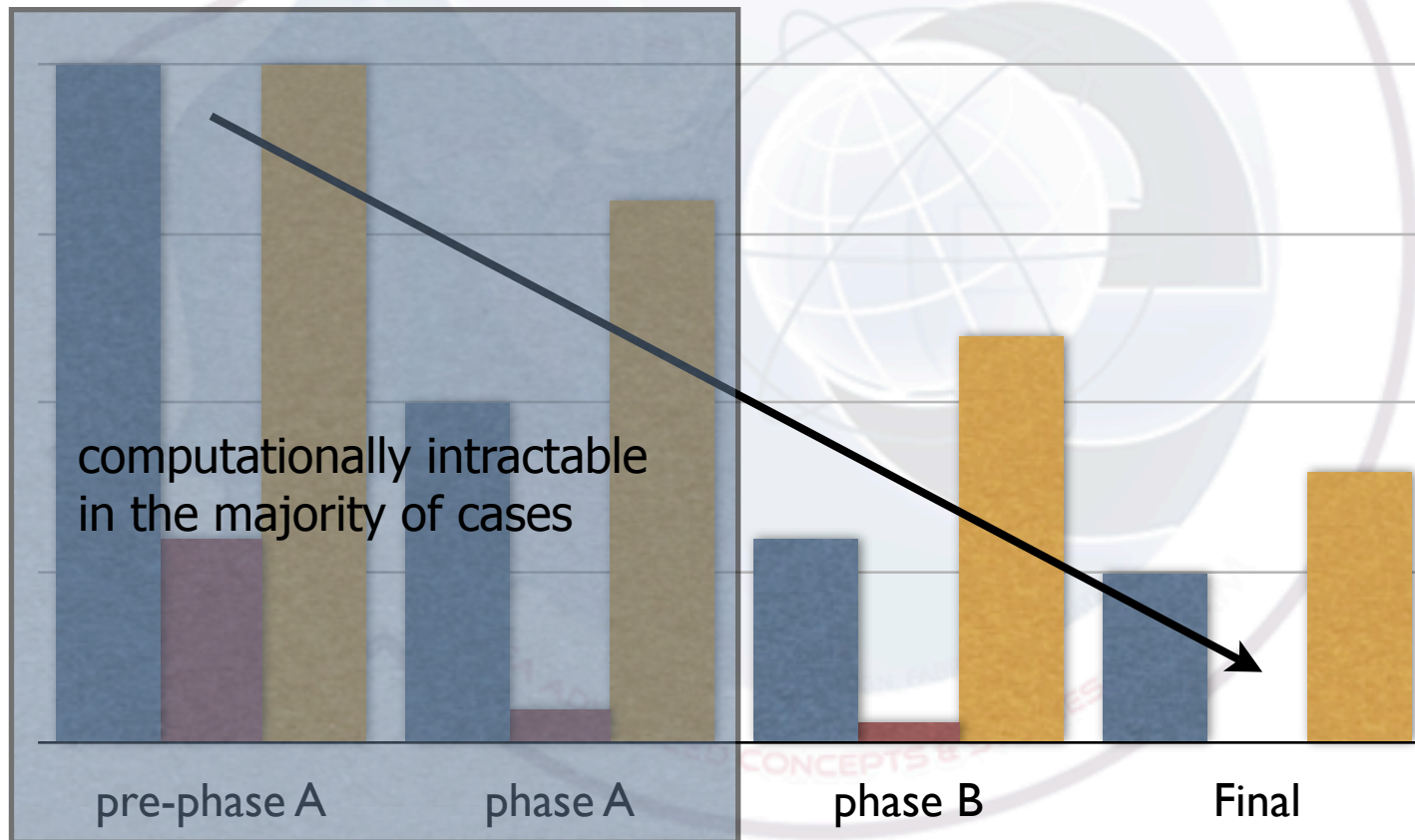


Mathematical programming

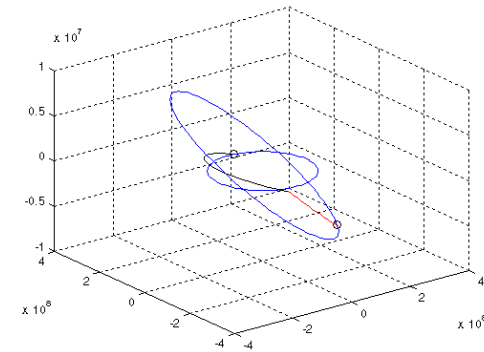
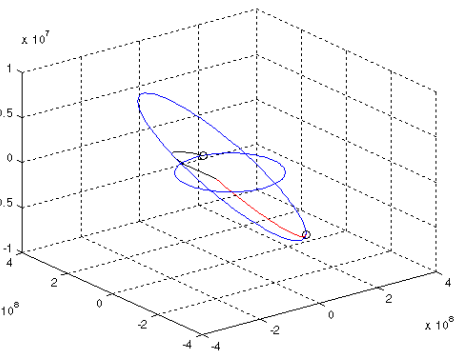
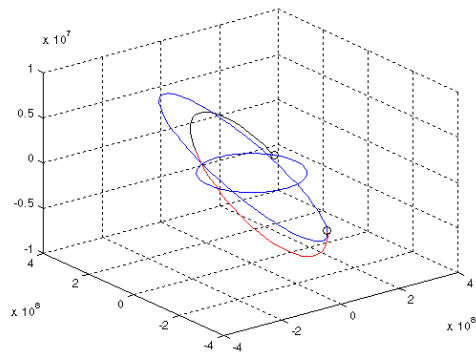
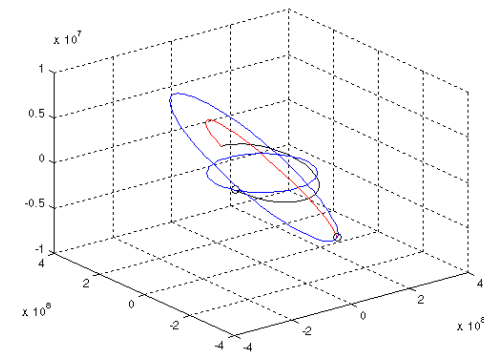
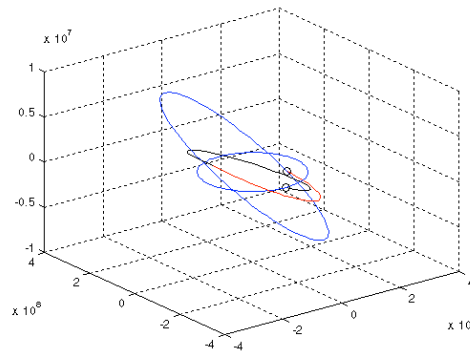
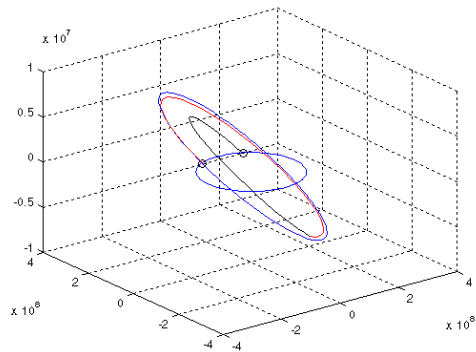
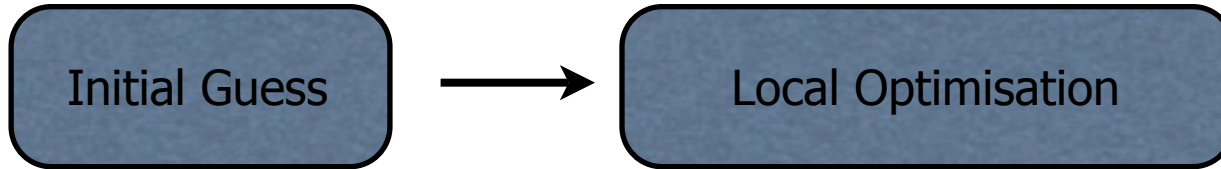
- There is no numerical algorithm able to tackle the mathematical programming problem in its generality
- The preliminary analysis of the problem structure suggests the most suited approach
- What makes the problem difficult/easy?
 - Dimensionality
 - Number of local minima
 - Topology of the feasible domain
 - Number of integer variables
 - Single or multiple objectives
 - Computational cost of the objective function evaluation
 - Convex or non convex constraints and objectives

Is trajectory optimisation difficult?

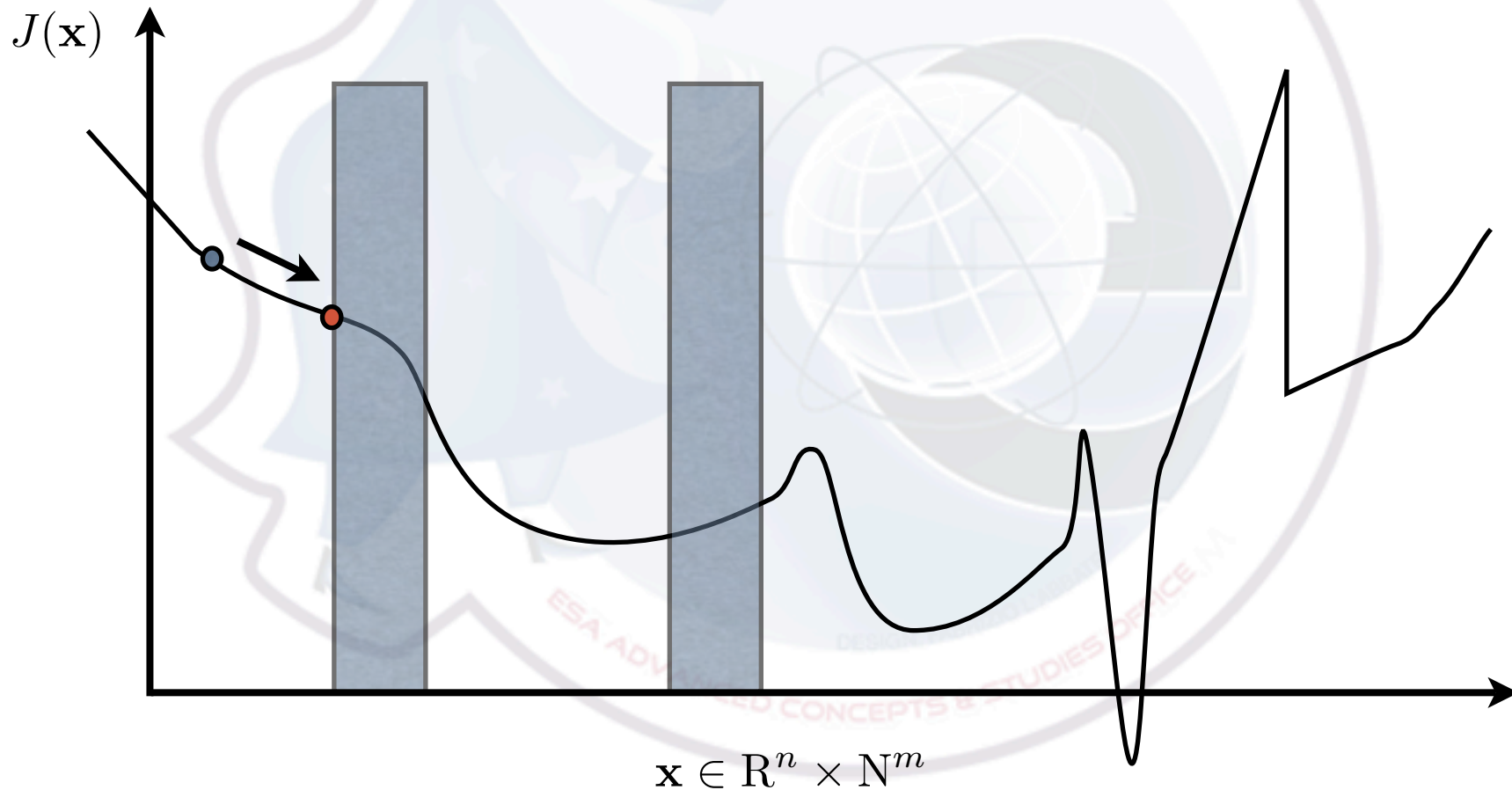
■ Local minima number
 ■ Integer variables
 ■ Landscape difficulty



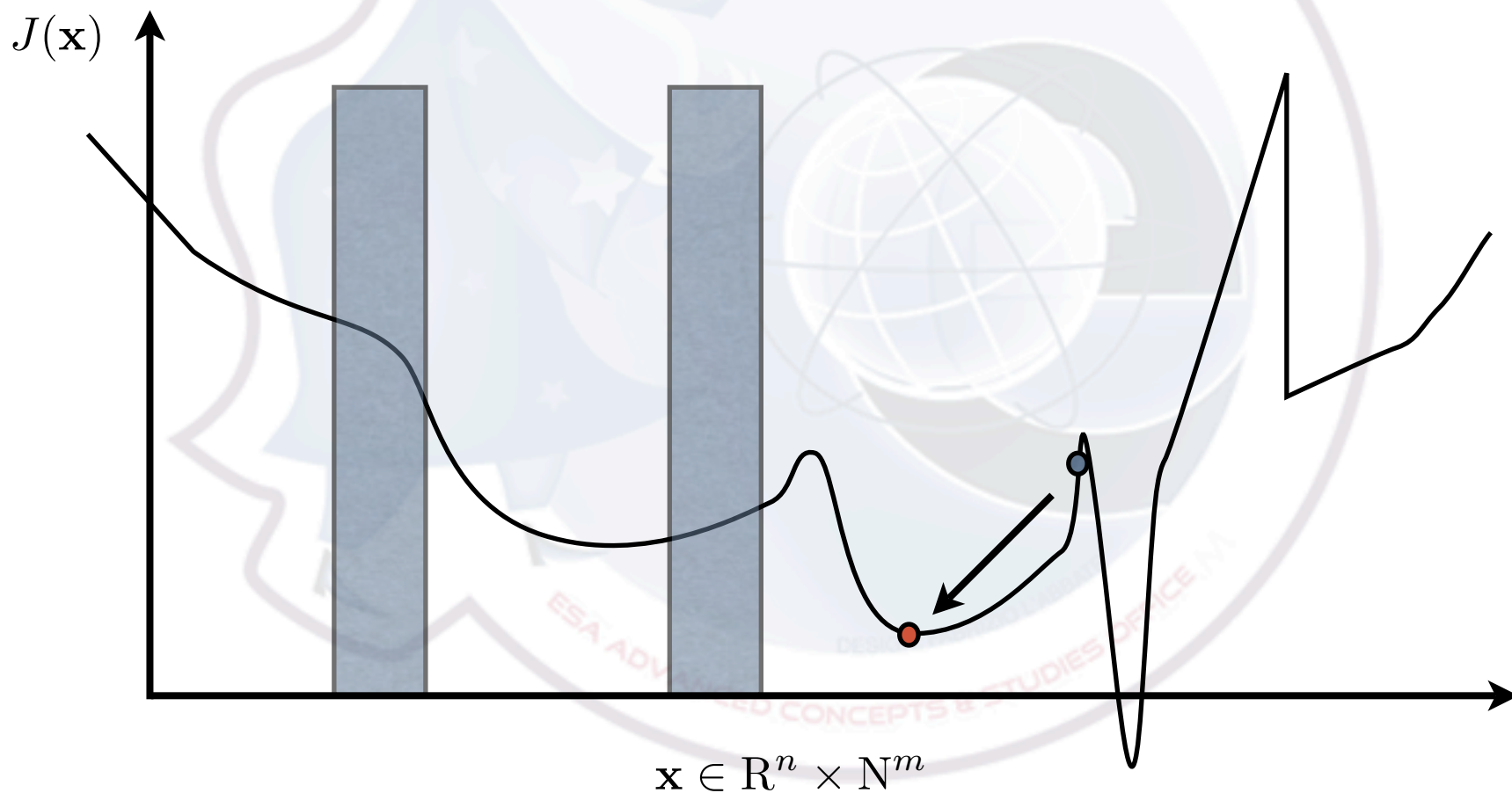
A schematic of the overall process



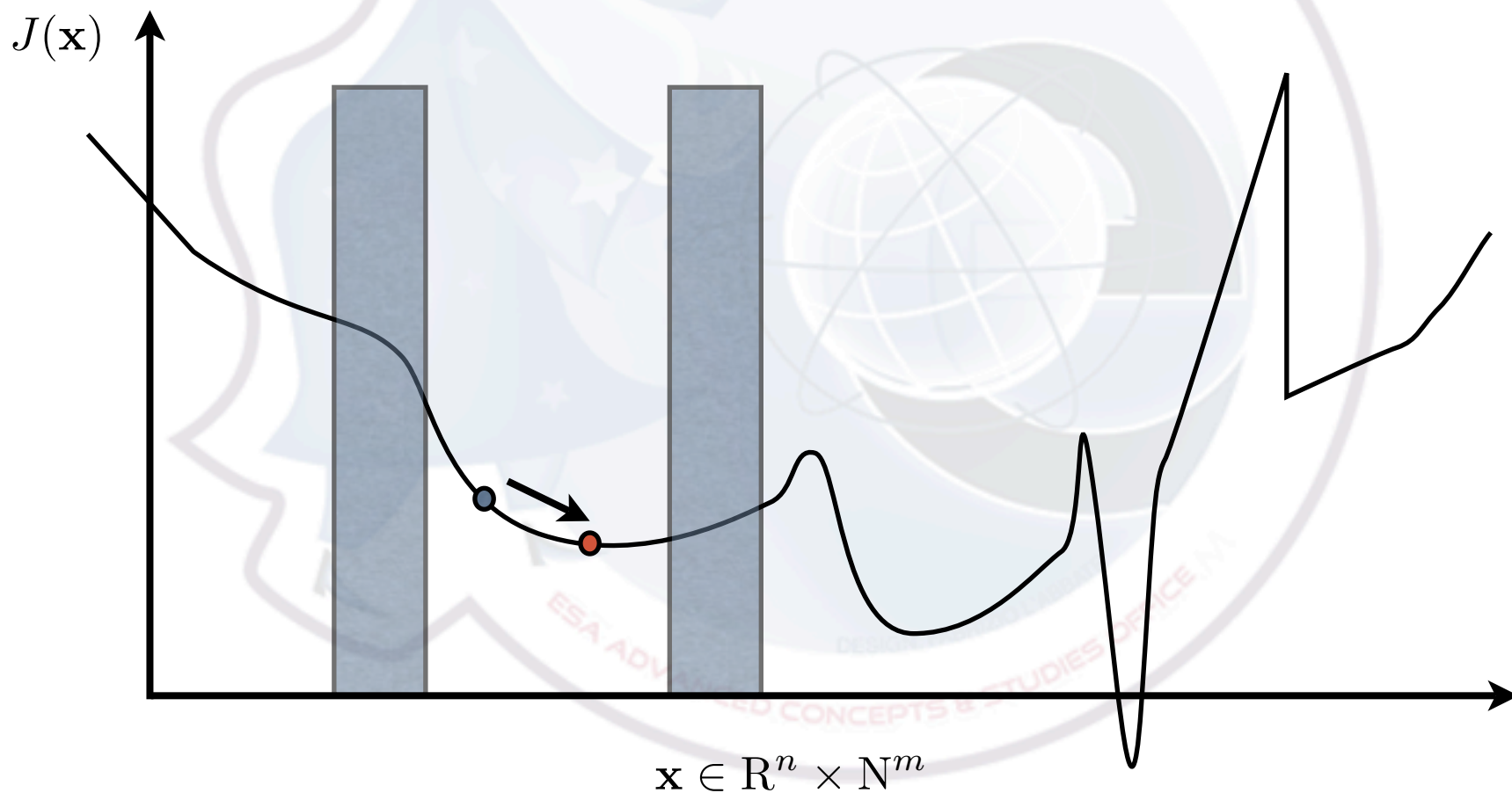
A schematic of the overall process



A schematic of the overall process

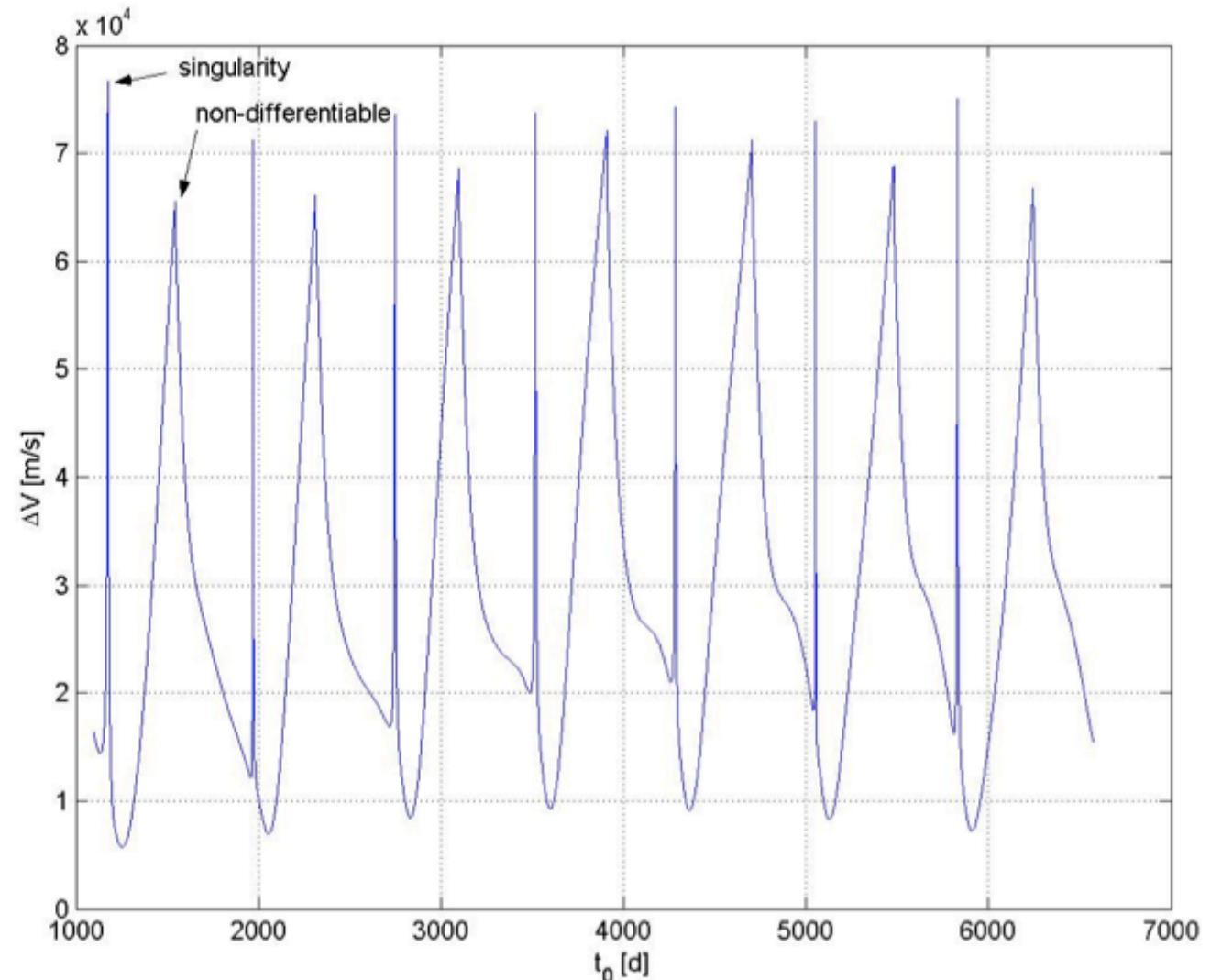


A schematic of the overall process



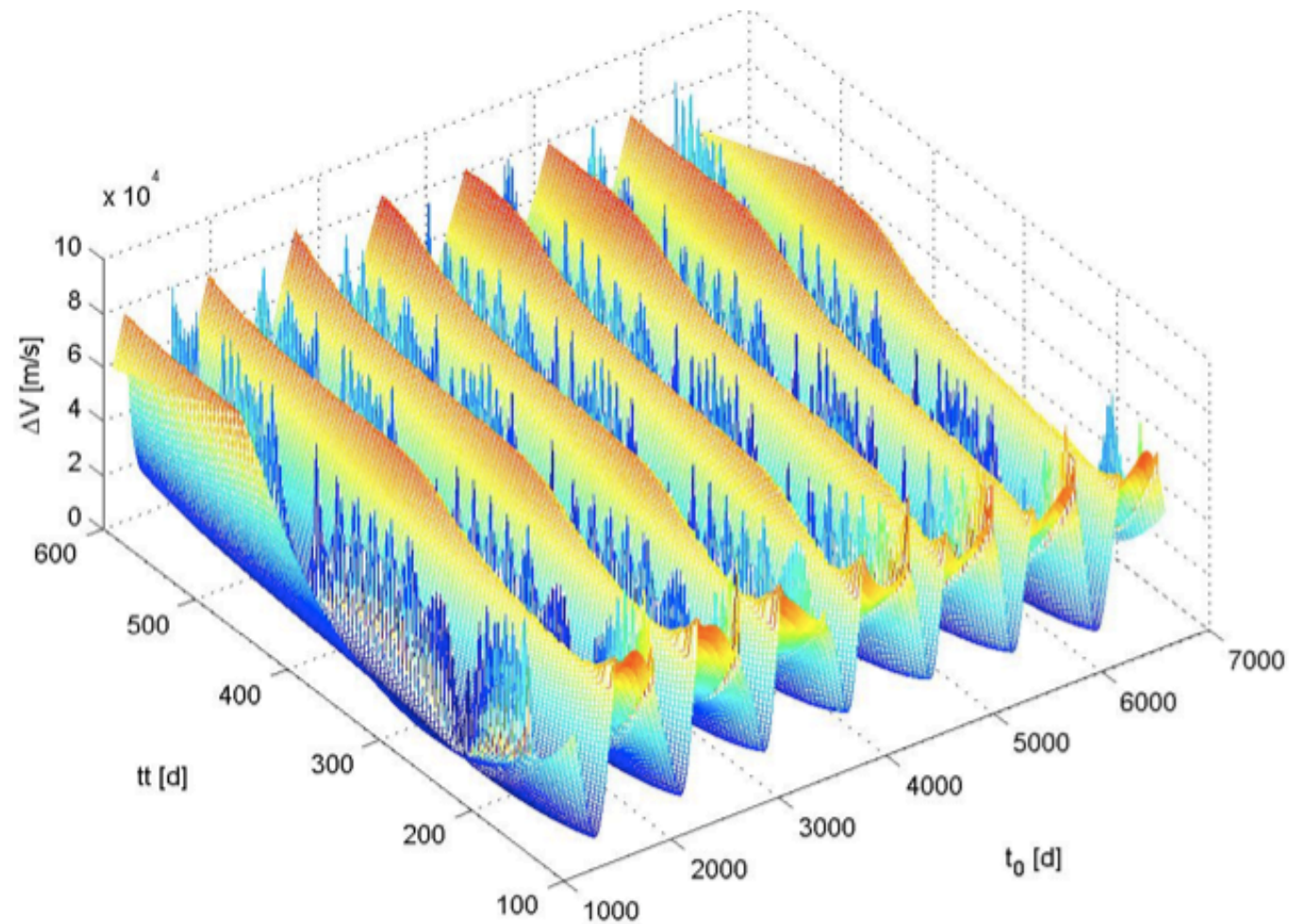
A "simple" example in 1D

- Earth-Mars transfer
- Chemical propulsion
- No deep-space manouvres
- 200 days of transfer
- MJD2000 used



A "simple" example in 2D

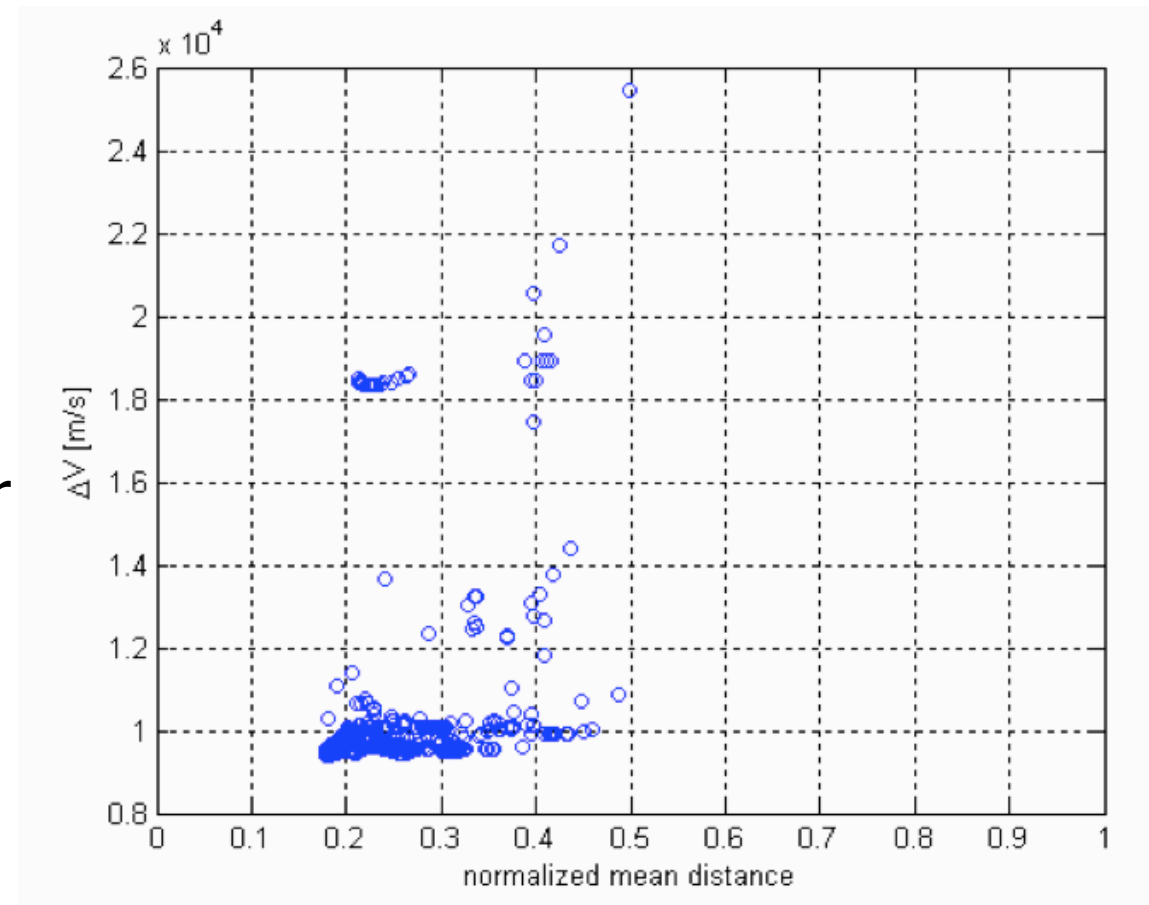
- Earth-Mars transfer
- Chemical propulsion
- No deep-space manouvres
- Days and MJD2000 used





A "simple" example in 3D

- Earth-Jupiter-Saturn transfer
- Chemical propulsion
- No deep-space manouvres
- Local optima cluster together
- Better local optima are close to the global one





Benchmarks

Open source code containing solvers and problems is available!!!



When we made them compete

- 🔗 September, 1st, 2005: GTOC1 announced
 - 🔗 Open to world wide academia, industry and researchers
- 🔗 October, 30th, 2005: Inscriptions closed
 - 🔗 17 Teams from Europe, China, Russia and the US
- 🔗 November, 7th, 2005: Problem released
 - 🔗 impact mission to TW229
 - 🔗 designed to assure the diversity of the solutions returned and the interest of the problem
- 🔗 December, 5th, 2005: Solutions returned
 - 🔗 Twelve out of the seventeen teams returned a solution
- 🔗 December, 20th, 2005: Solutions checked and definitive rankings formed
 - 🔗 Only one solution could not be ranked
- 🔗 February, 2nd, 2006: Workshop on Global Trajectory Optimisation
 - 🔗 All the teams presented their methodologies and discussed upon the most promising trajectory optimisation researches

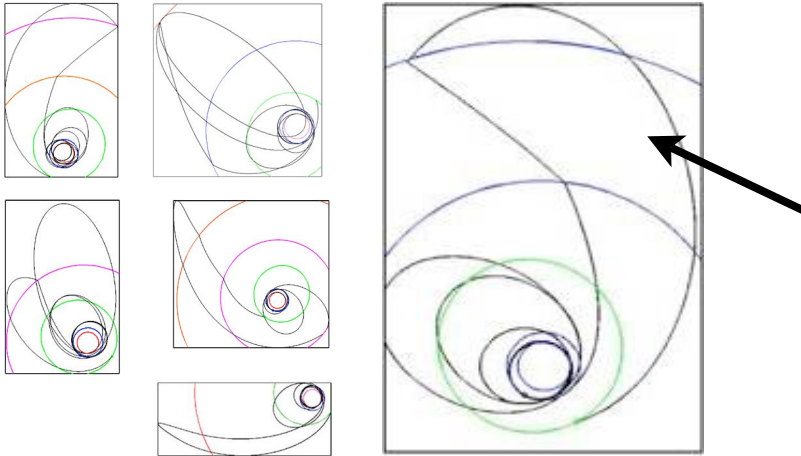


GTOC Trophy

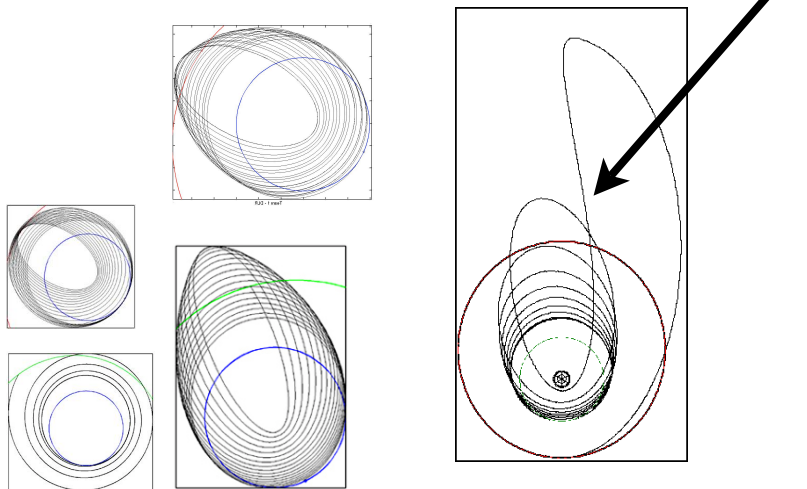
[Competition official home page](#)

[Special issue of Acta Astronautica](#)

Final ranks (GTOC1)

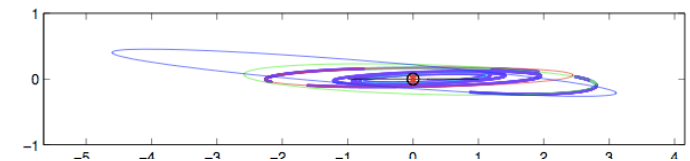
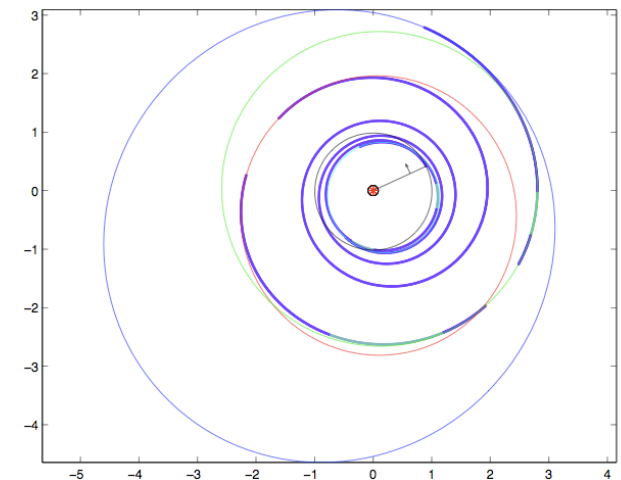


| | Team name | Value |
|---|-------------------------------------|-----------|
| G | JPL (Team 11) | 1,850,000 |
| G | Deimos Space (Team 17) | 1,820,000 |
| G | GMV (Team 2) | 1,455,000 |
| L | Moscow Aviation Institute (Team 12) | 1,364,000 |
| L | Politecnico di Torino (Team 4) | 1,290,000 |
| L | CNES/CS (Team 7) | 1,194,000 |
| G | Glasgow University (Team 13) | 385,000 |
| L | Moscow University (Team 9) | 351,152 |
| L | Alcatel (Team 14) | 330,385 |
| G | DLR (Team 1) | 330,000 |
| G | Tsinghua University (Team 8) | 89,000 |



And when we competed....

- The winner of the first edition (Jet Propulsion Laboratory) organized a second edition
- A grand asteroid tour was given as a problem
 - Four groups of many asteroids and a trajectory to reach them all....
 - 90 days of minimum stay on each asteroid
 - Low-thrust propulsion 0.1N NEP
 - Initial mass 1500 kg
 - Departure DV 3.5 km/sec
 - Minimisation of mass/time
- Thanks to Anastassios Petropoulos and to JPL for having organized the second edition!!



Winning trajectory from Turin Polytechnic

Final ranks (GTOC2)

| Rank | Team | J (kg/yr) |
|------|--|--------------------|
| 1 | 4: Politecnico di Torino | 98.64 |
| 2 | 13: Moscow Aviation Institute, and Khrunichev State Research and Production Space Center | 87.93 |
| 3 | 10: Advanced Concepts Team, ESA | 87.05 |
| 4 | 15: Centre National d'Etudes Spatiales (CNES) | 85.43 |
| 5 | 1: GMV Aerospace and Defence | 85.28 |
| 6 | 2: German Aerospace Center (DLR) | 84.48 |
| 7 | 9: Politecnico di Milano | 82.48 |
| 8 | 19: Alcatel Alenia Space | 76.37 |
| 9 | 14: Moscow State University | 75.08 |
| 10 | 7: Tsinghua University | 56.87 |
| 11 | 18: Carnegie Mellon University, J.J. Arrieta-Camacho | 27.94 |
| – | 17: University of Glasgow, <i>et al.</i> | 73.87 ^a |
| – | 21: Technical University of Delft and Dutch Space | 15.95 ^b |
| – | 23: Facultes Universitaires Notre-Dame de la Paix (FUNDP) | – ^c |
| – | 26: University of Maribor, Bostjan Eferl | – ^d |

^a Significant position and velocity violations at the asteroids and Earth

^b Significant position and velocity violations at the asteroids and Earth, and flight time limit violation

^c Only one leg computed (Earth to Group 4)



Interaction with the european academia: the Ariadna projects





Cooperation with academia via Ariadna

- 
2003 - Advanced global optimisation tools for mission analysis and design
 - 
 4101a - Myatt, D.R., Becerra, V.M., Nasuto, S.J., and Bishop, J.M., Reading University and Goldsmith College
 - 
 4101b - Di Lizia, P., Radice, G., Glasgow University

- 
2005 - Spiral trajectories in Global Optimisation of Interplanetary and Orbital Transfers
 - 
 4106 - Vasile, M., Schutze, O., Junge, O., Radice, G., and Dellnitz, M., Glasgow University and Paderborn University

- 
2006 - Global trajectory optimisation: Can we prune the solution space when considering deep space manouvres?
 - 
 4110a - Ecole de Mines
 - 
 4110b - Politecnico di Milano and Michigan University
 - 
 4110c - Glasgow University and Reading University



Off the shelf GO algorithms



Which algorithms?

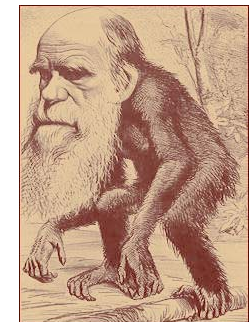
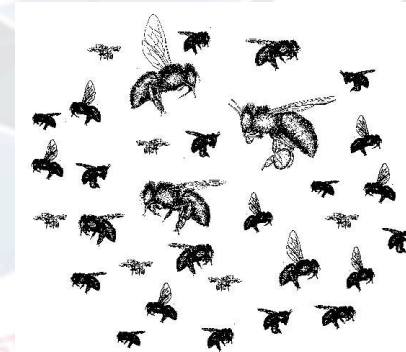
Stochastic

- Genetic algorithms and variants
- Simulated Annealing (simple and adaptive)
- Particle Swarm and variants
- Differential Evolution (the 7 types)
- Monte Carlo
- Ant Colony over continuous space (Dorigo's version)
- GLOBAL
- others....



Deterministic (or quasi)

- DIRECT
- Multi Coordinated Search
- others....



What problems?

MGA problem

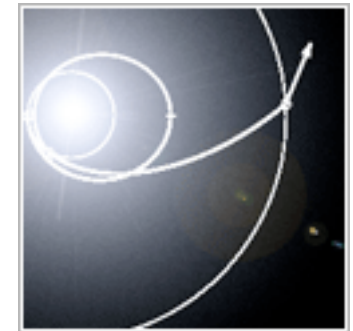
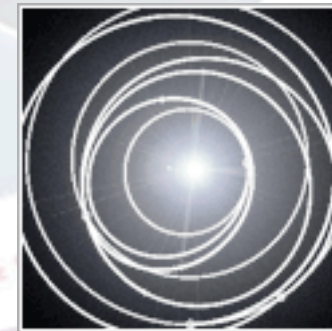
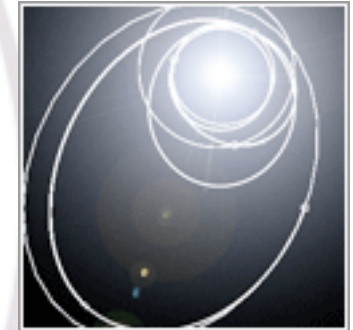
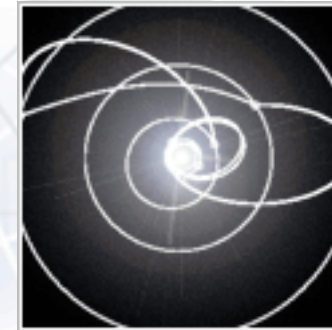
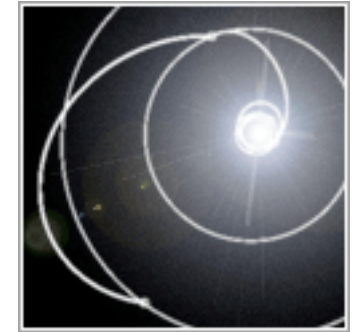
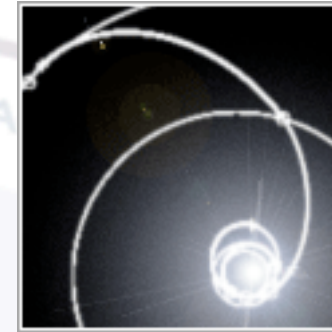
- Cassini
- Apophis Deflection
- GTOC1, with different sequences

MGA with DSM problem

- Cassini
- Messenger with no mult. rev.
- Rosetta
- SAGAS

MGA with simplified low-thrust shapes

- Multiple asteroid rendezvous mission





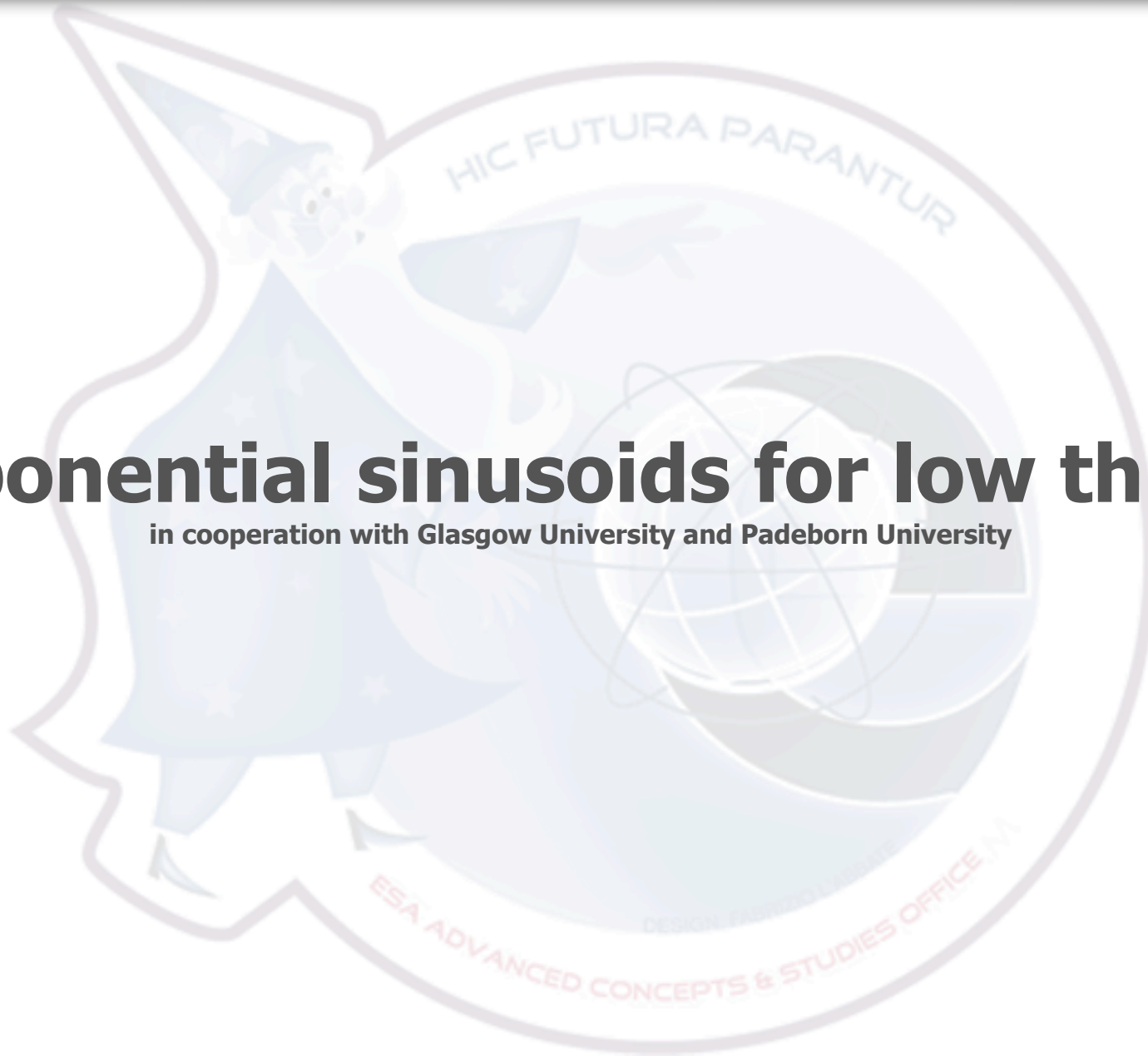
Lesson Learned?

- Algorithms are difficult to compare
- We can say that for complex problems no simple algorithm work
- DE, PSO, GA and ASA have attractive characteristics for different problems. Our favorite is certainly DE
- A cooperative approach, implemented both in our distributed computing environment and in a single computer, allow to find good solutions by just 'pressing a button'



Exponential sinusoids for low thrust

in cooperation with Glasgow University and Paderborn University





Going from A to B with low-thrust

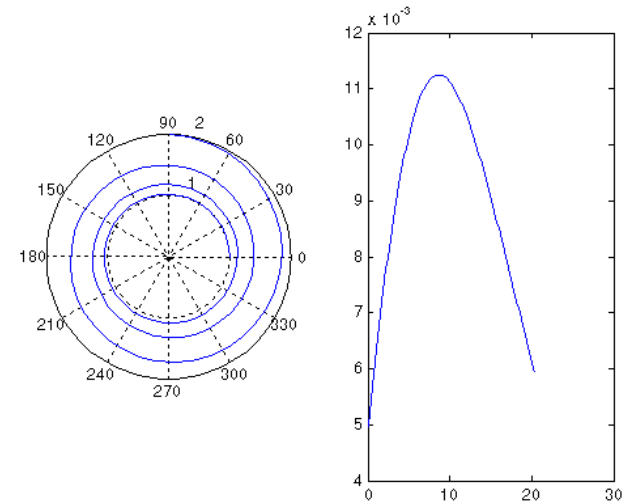
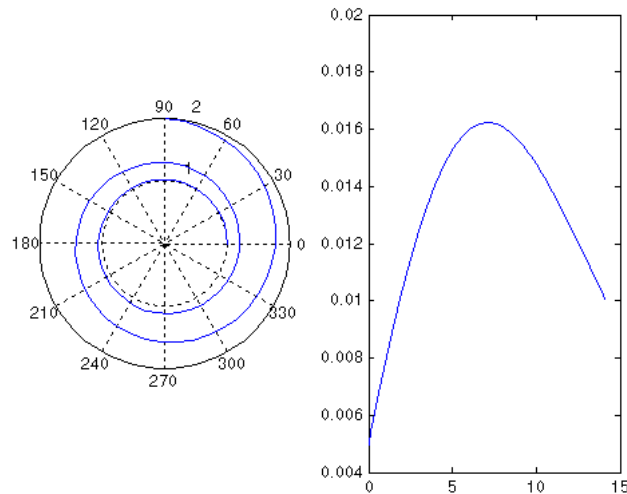
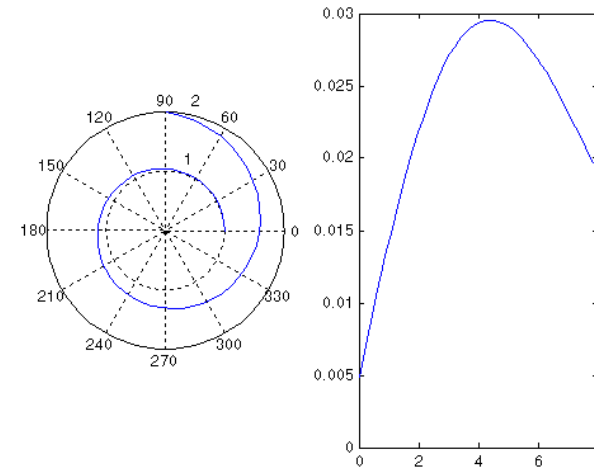
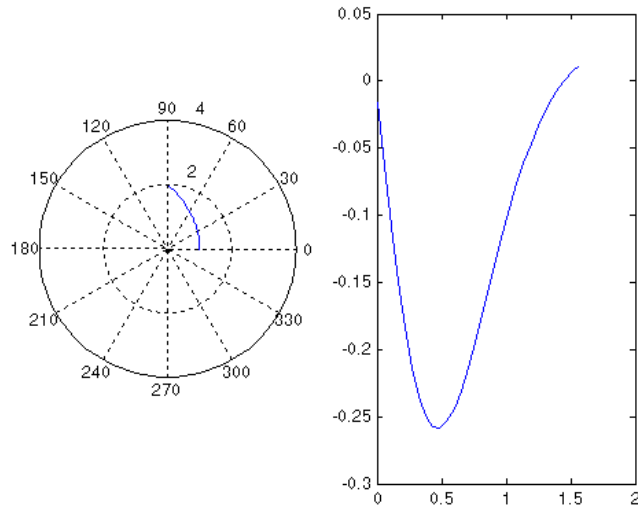
- Taking into account that A and B are moving.....
- For low-thrust arcs there is no simple solution..... An infinite number of trajectories lead from A to B!!! We therefore consider only a restricted class:

$$\begin{cases} \ddot{r} - r\dot{\theta}^2 + \mu/r^2 = F \sin \alpha \\ \ddot{\theta}r + 2\dot{\theta}\dot{r} = F \cos \alpha \end{cases}$$

$$r = k_0 \exp[k_1 \sin(k_2\theta + \varphi)] \longrightarrow \text{Exponential Sinusoids}$$

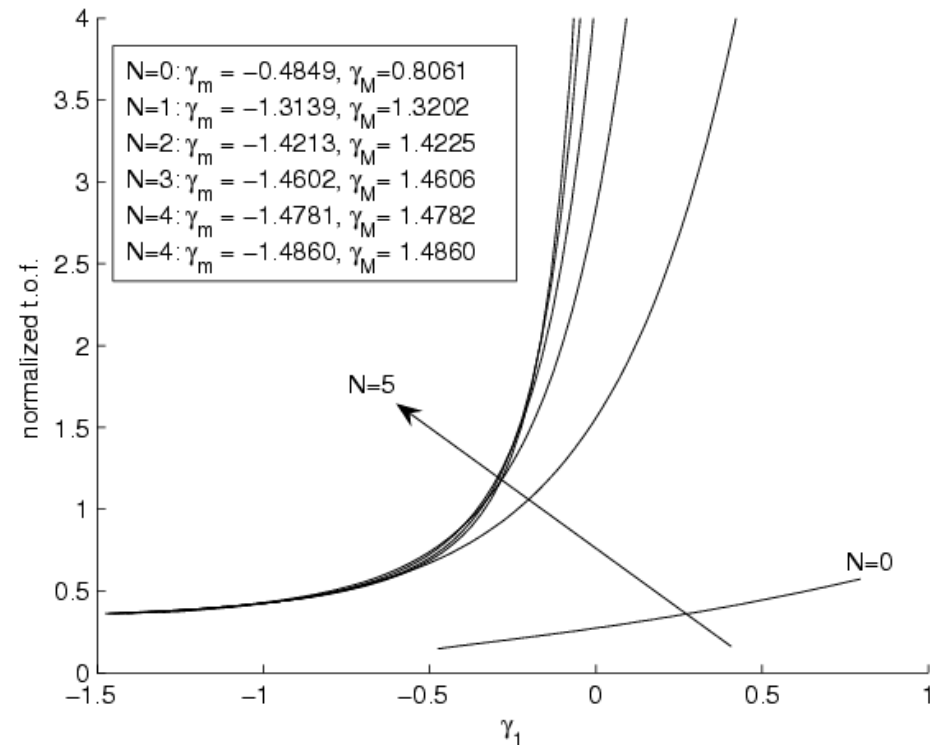
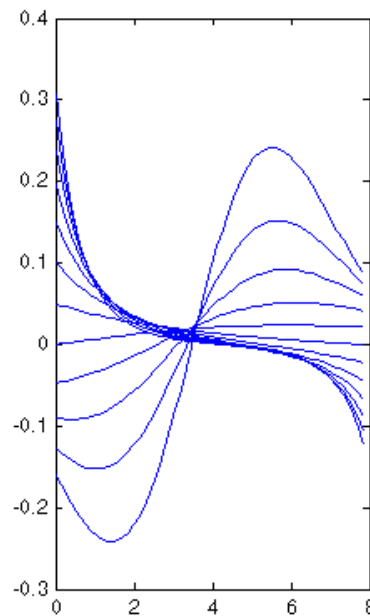
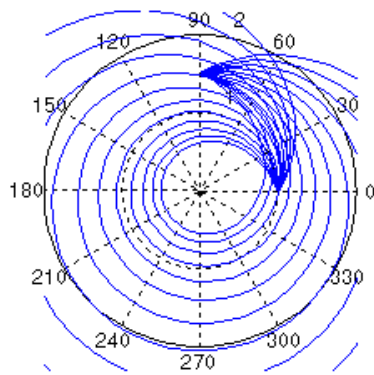


Going from A to B.....



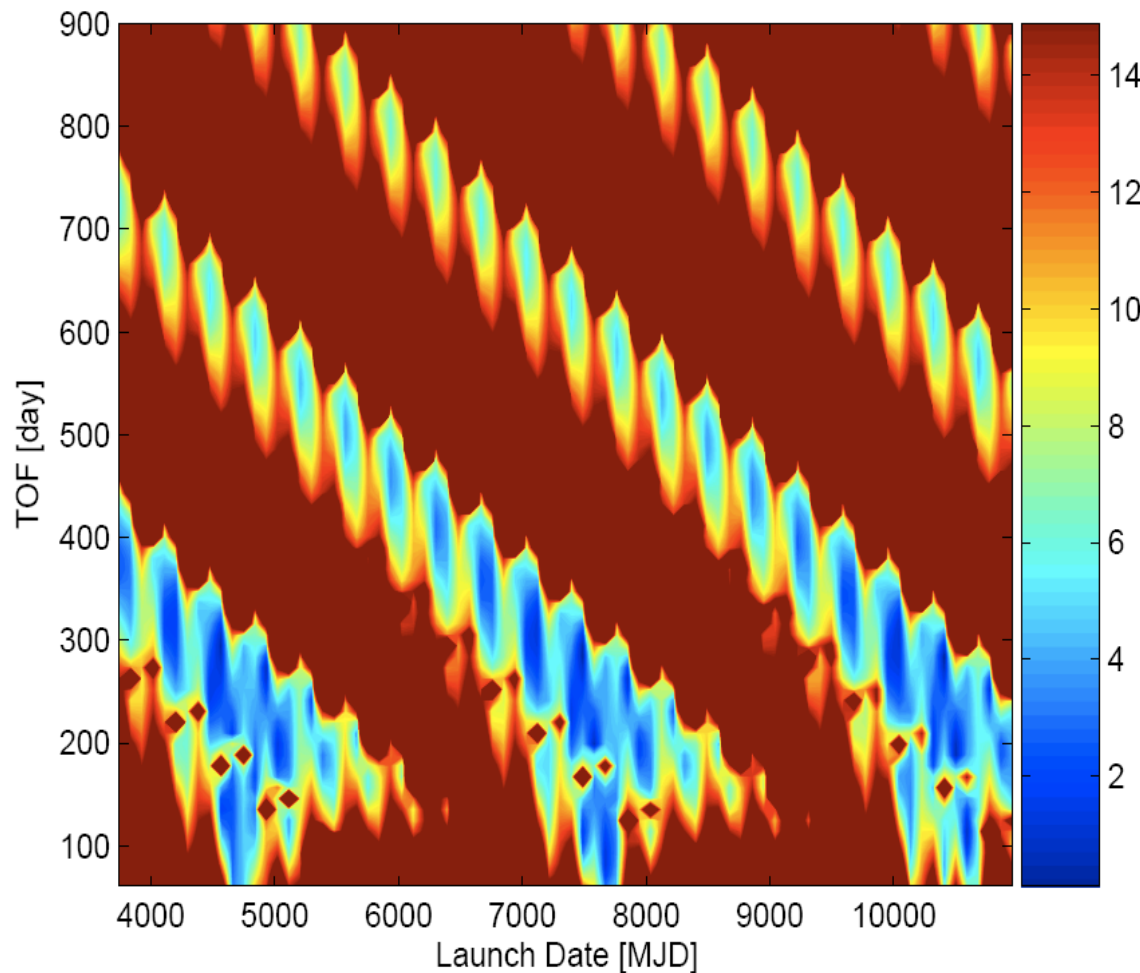
Good choice?

- We may restate Lambert's problem in a slightly different form (there may be no solution) and solve it efficiently (see graph below)
- Typical high thrust.
- Impossible to vary the boundary conditions



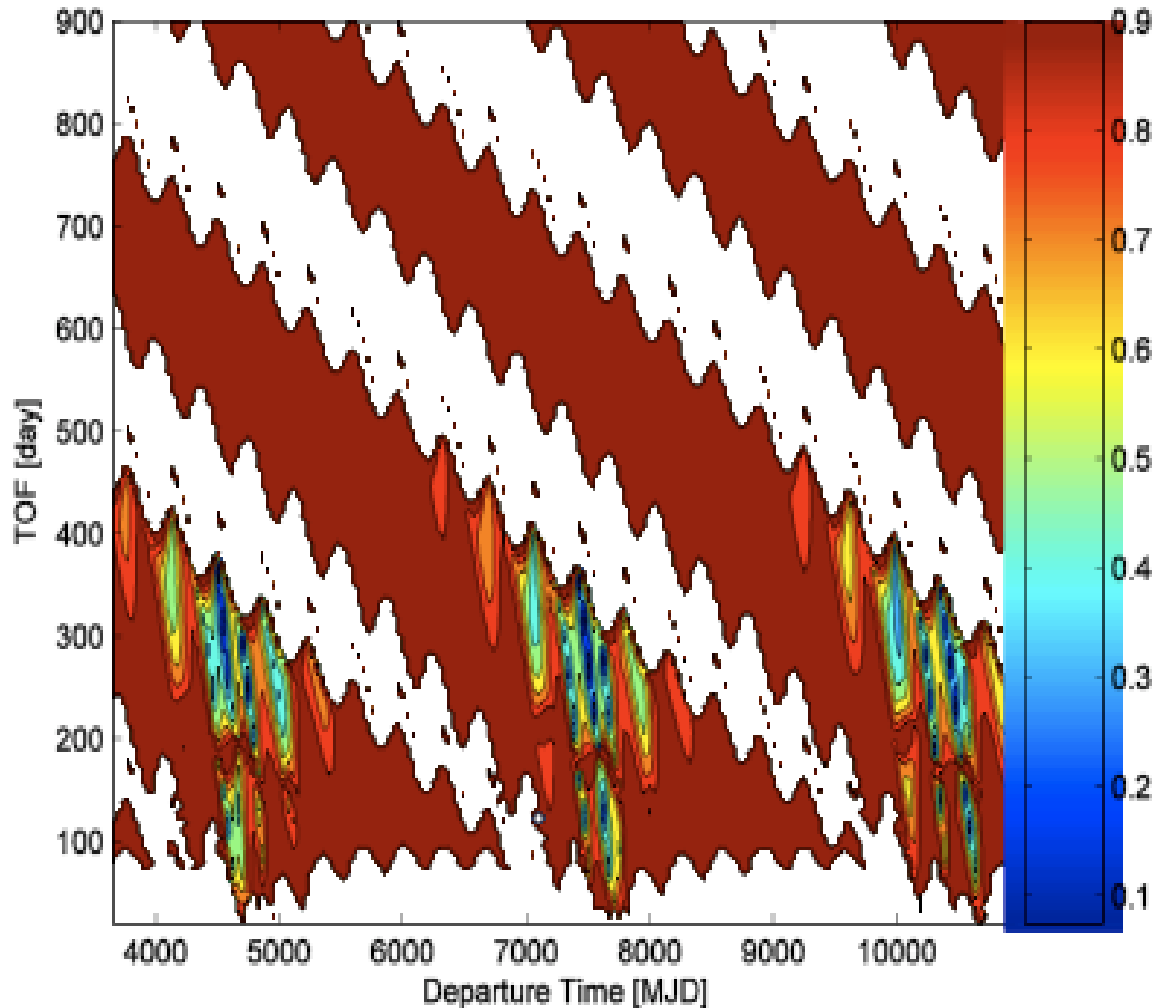


Good choice?



For $N=0$ no substantial advantages with respect to Lambert arcs! For $N>1$ exponential sinusoids are a possibility

Good choice?



For $N=0$ no substantial advantages with respect to Lambert arcs! For $N>1$ exponential sinusoids are a possibility



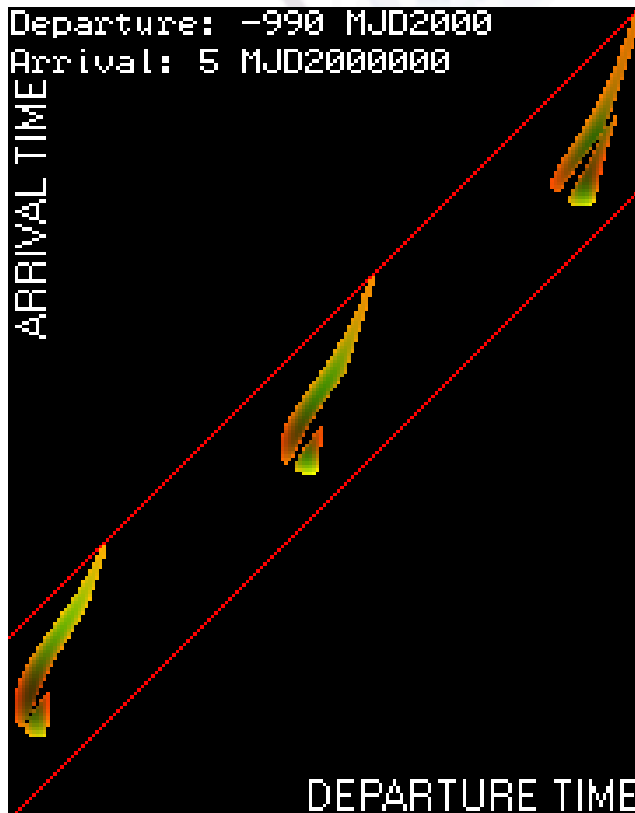
GASP!

**Gravity Assist Space Pruning
In cooperation with Reading University**

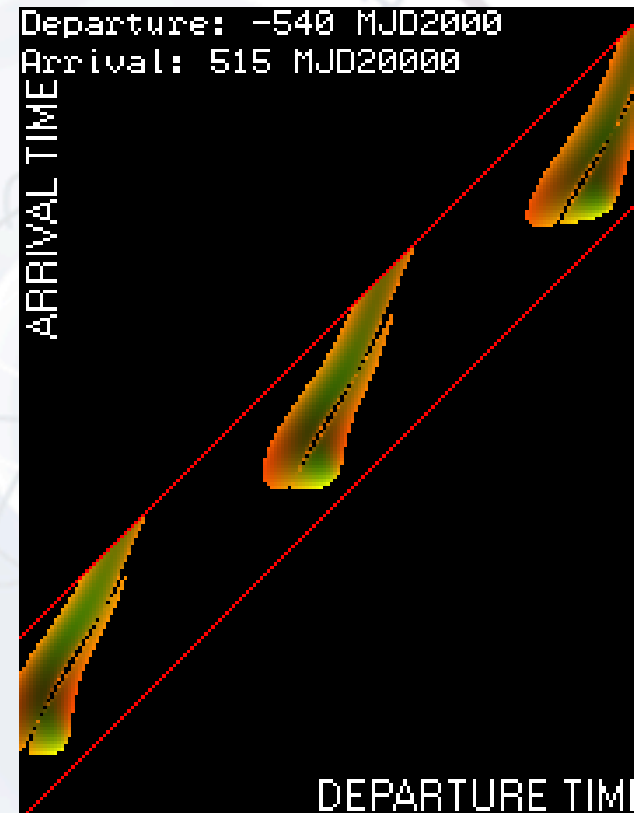
Overview of Gravity Assist Space Pruning

- Deterministic algorithm
- Transforms the N dimensional space into a cascade of 2D spaces
- Exploits domain knowledge to effectively constrain space
- User defined constraints on launch energy, gravity assist thrusts, swing-by periapsis radii, and braking thrust
- Provides intuitive visualisation of high dimensional MGA search spaces
- Allows simple identification of solution families
- Produces a set of reduced box bounds (between 6 and 9 orders of magnitude smaller than original space)

Effect of launch velocity constraint



pruned at 5km/sec



pruned at 10km/sec

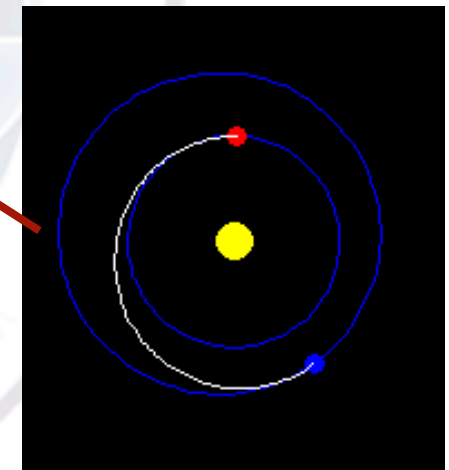
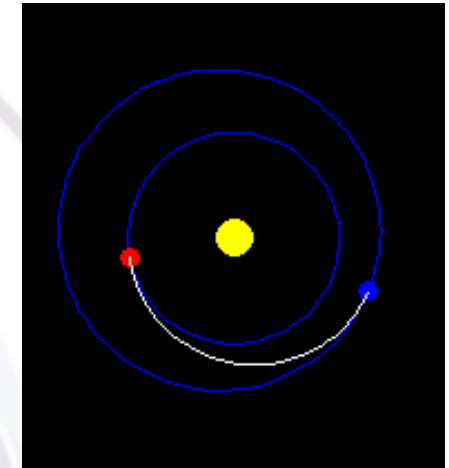
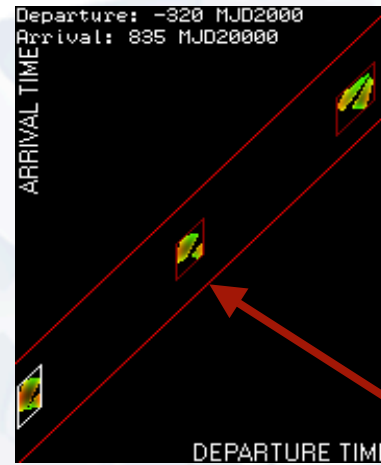
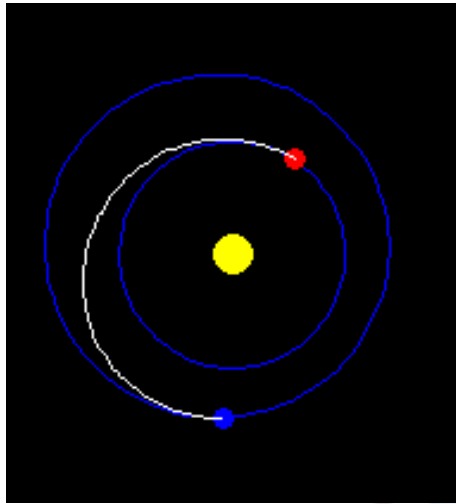
Note: Arrival time = Departure time + transfer time ($t_0 + T_1$)

Adding a Braking Constraint

- Adding a braking manoeuvre constraint at Mars of 5 km/s yields only 4% of the search space valid.

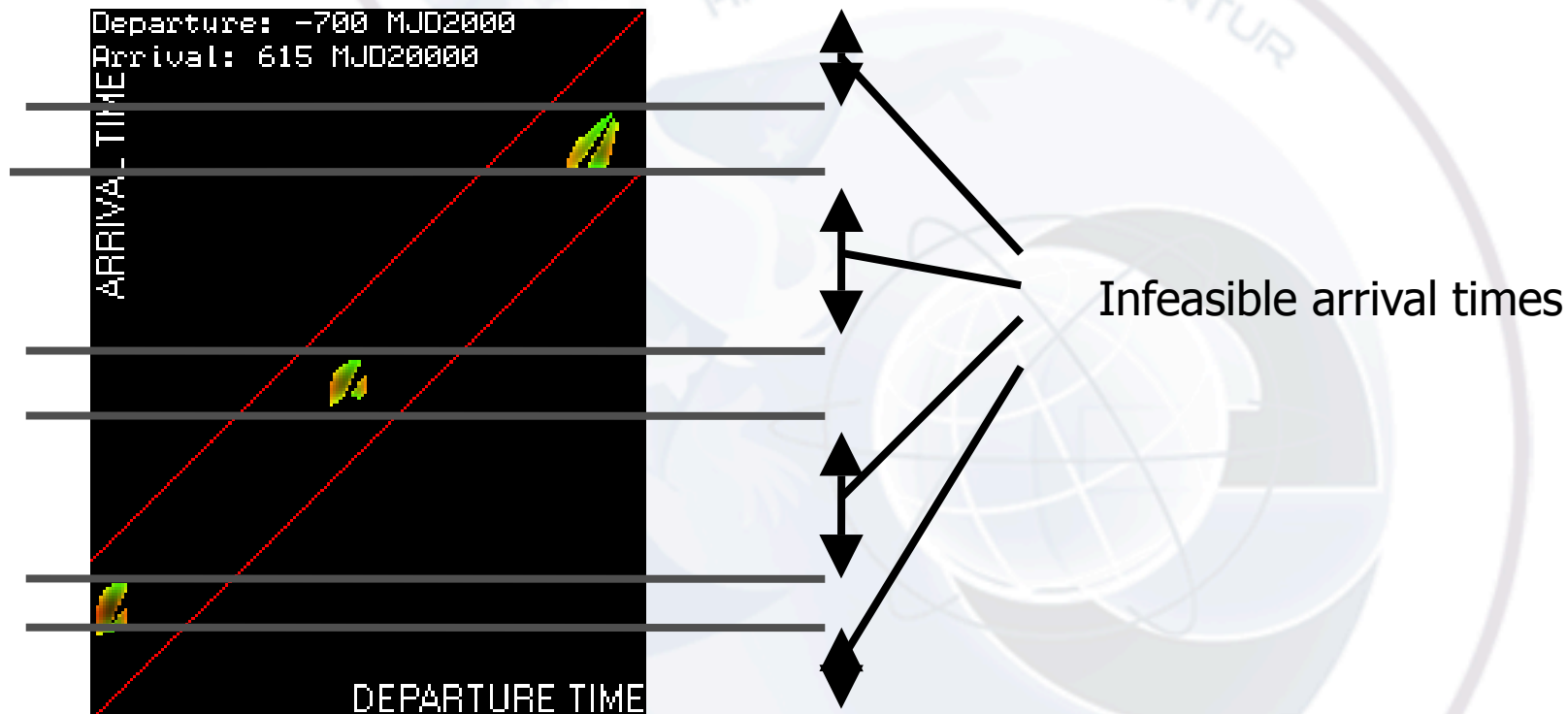


Optimising launch windows



- Reduced box bounds automatically calculated for each launch window
- Each launch window can be optimised separately using a global optimisation scheme, e.g. Differential Evolution
- Different solution families can be examined separately and then the most appropriate chosen

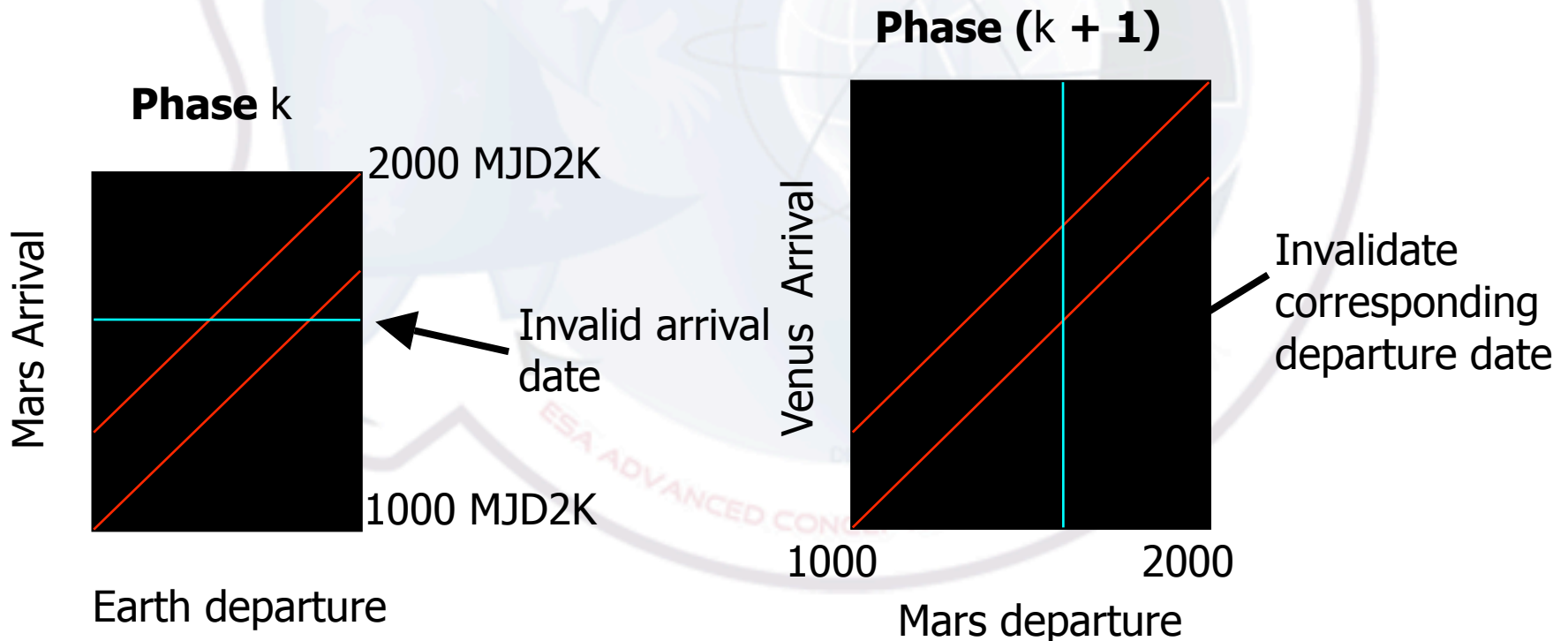
Two and more phases...



Therefore, it must be infeasible to depart from the next planet on these dates...

Forward constraining

- Infeasible arrival date constrains departure from the planet on that date
- Horizontal axis constrains vertical in the next phase



Complete GASP Algorithm

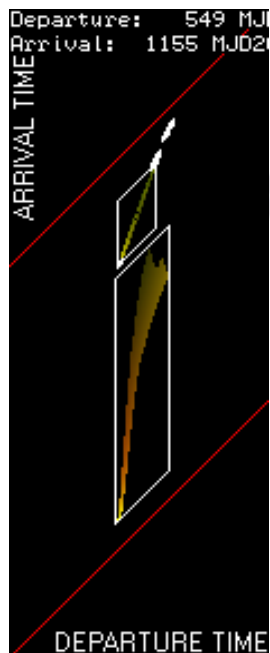
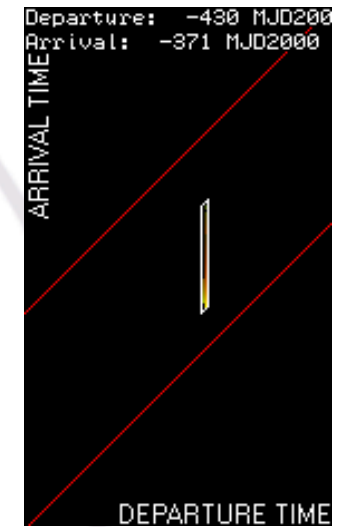
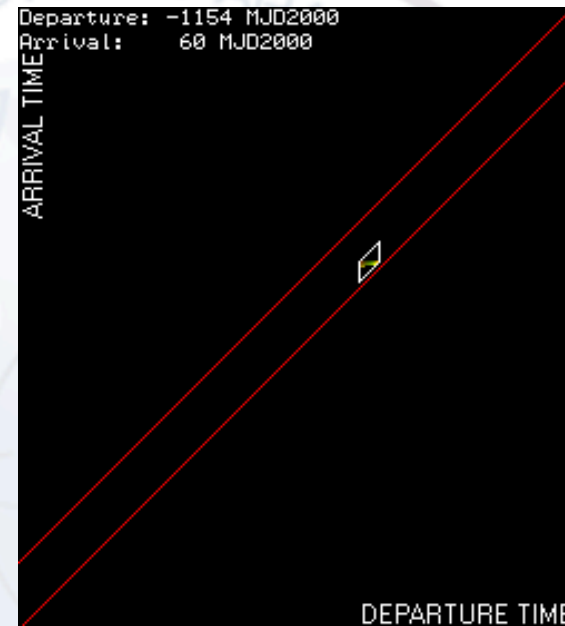
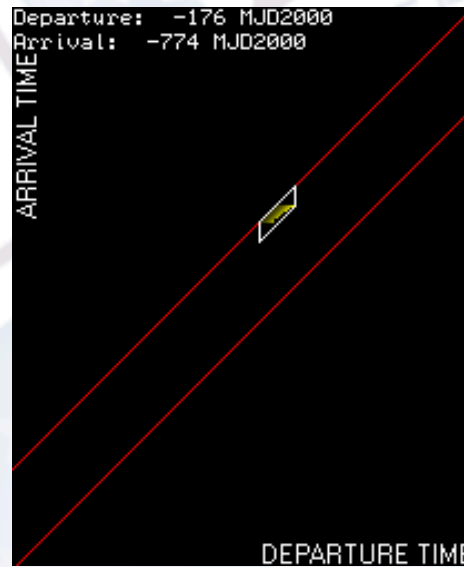
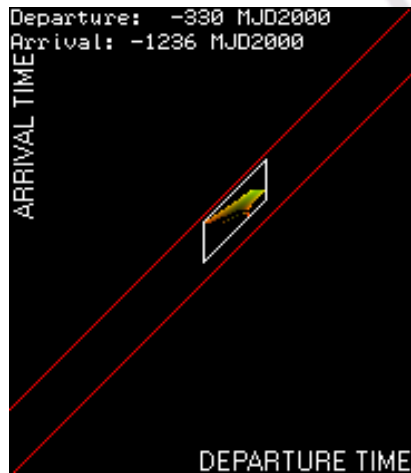
- Perform sampling as sequence of 2D spaces
 - Earth departure/Mars arrival
 - Mars departure/Venus arrival
- Apply initial velocity constraint to first phase
- Forward constraining through all phases
- Apply braking manoeuvre constraint
- Backward constraining through all phases
 - Invalidate arrival dates based on departure dates



Scaling of GASP algorithm

- GASP algorithm scales polynomially – this is due to the characterisation of the search space as a sequence of connected 2D search spaces
- This is true both in memory requirements and computational expense
- Copes well with the curse of dimensionality

EVVEJS With New Bounds



- We apply Differential Evolution to the reduced bounds
- Best solution is 4932.2 m/s
- Launch velocity: 3737m/s
- Probe velocity: 1488 m/s
- A direct transfer requires launch velocity of approx 10000m/s

