

# Team 9

## Moscow State University

### Department of Mechanics and Mathematics

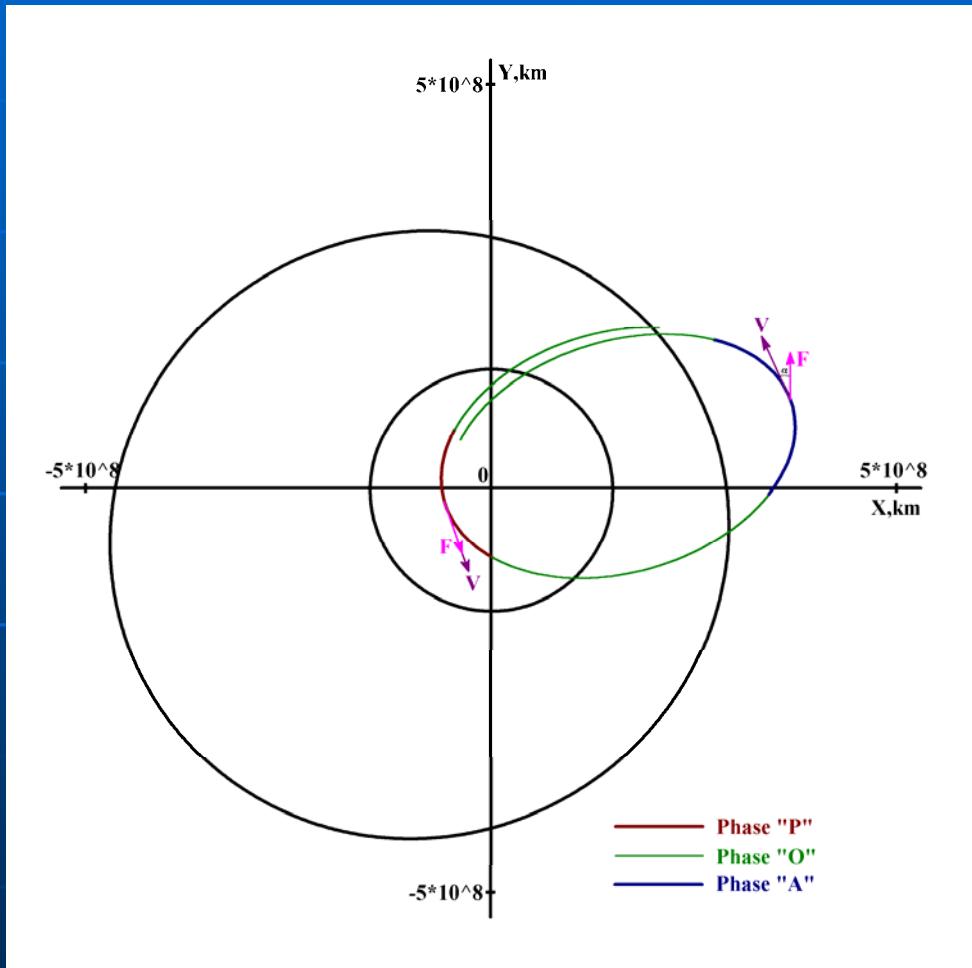


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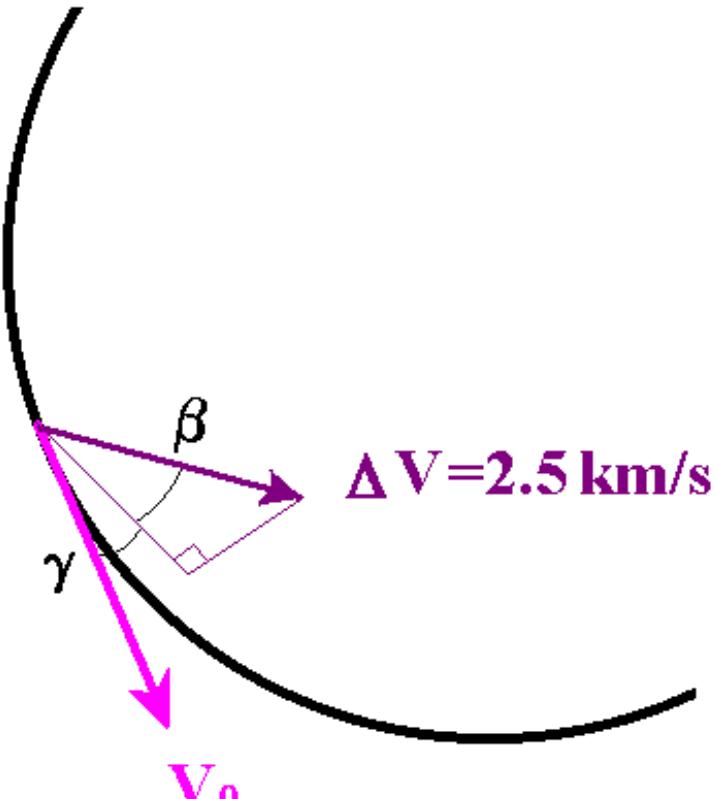
- Optimal control problem ->  
-> *maximum principle* ->
- Boundary value problem ->  
-> *shooting method* ->
- System of nonlinear algebraic equations

- $\alpha$  - the angle between the thrust vector and the SC velocity vector
- $\theta_a, \theta_\pi$  - limits of instant true anomaly  
 $|\theta| \leq \theta_\pi, |\theta| \geq \theta_a$
- $T_0, T_1$  – the start time and the finish time



# Impulse parameters

$\beta, \gamma$  - the angles which define direction of an initial impulse



# Conditions

$$\vec{R}_{SC}(T_1) = \vec{R}_{AS}(T_1)$$

$$\min R_{SC} = 0,2AU$$

Parameters to meet the conditions:

$$\alpha, \beta, \gamma, T_1$$

# parameters value

$$\alpha = 2.8110$$

$$\beta = 0.1106$$

$$\gamma = -0.0410$$

$$\theta_a = 2.8349$$

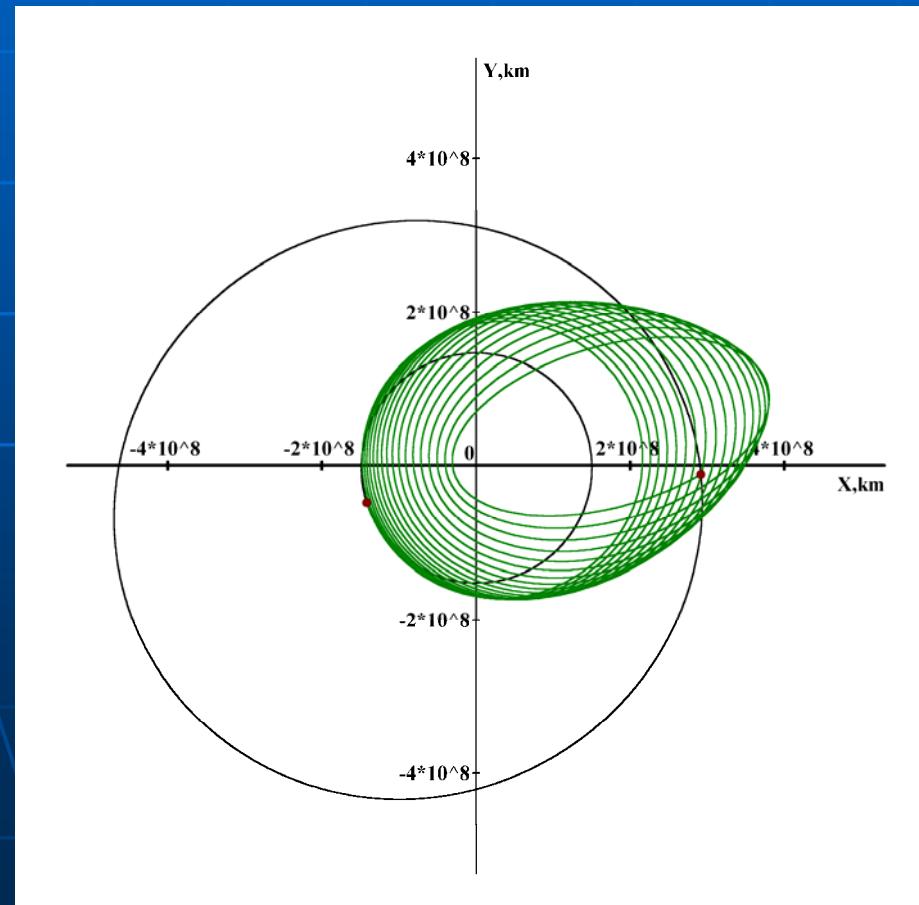
$$\theta_{\pi} = 1.2993$$

$$T_0 = 7038 \text{ MJD}$$

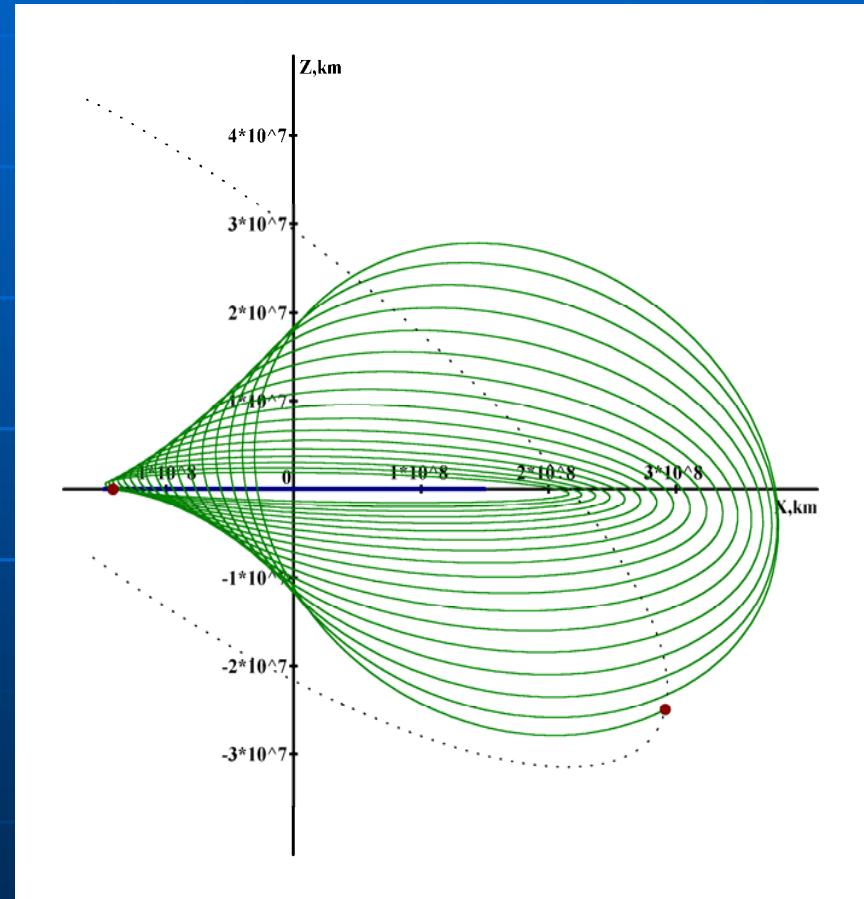
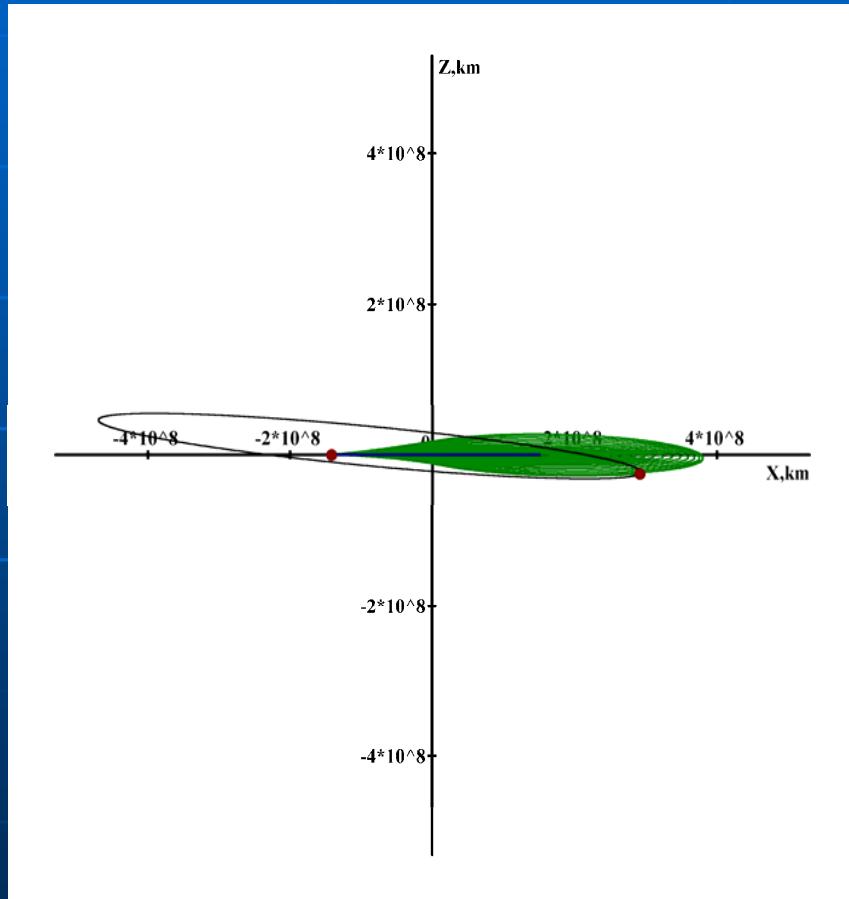
$$T_1 - T_0 = 10323.3 \text{ D}$$

# Trajectory projection to Sxy - plane

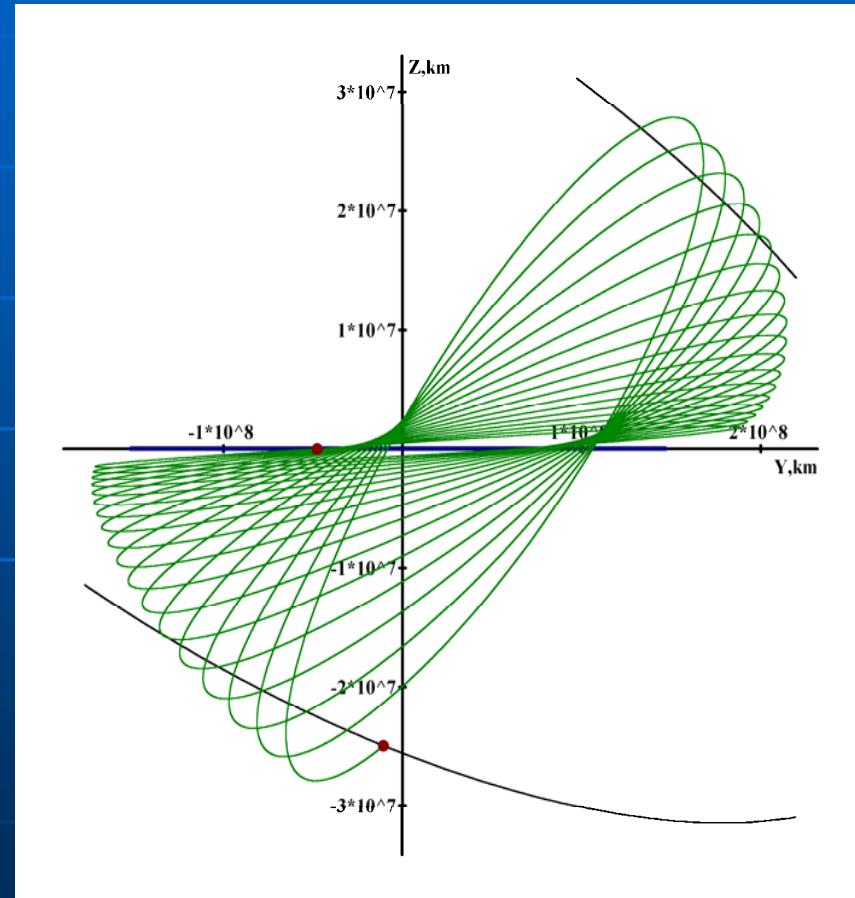
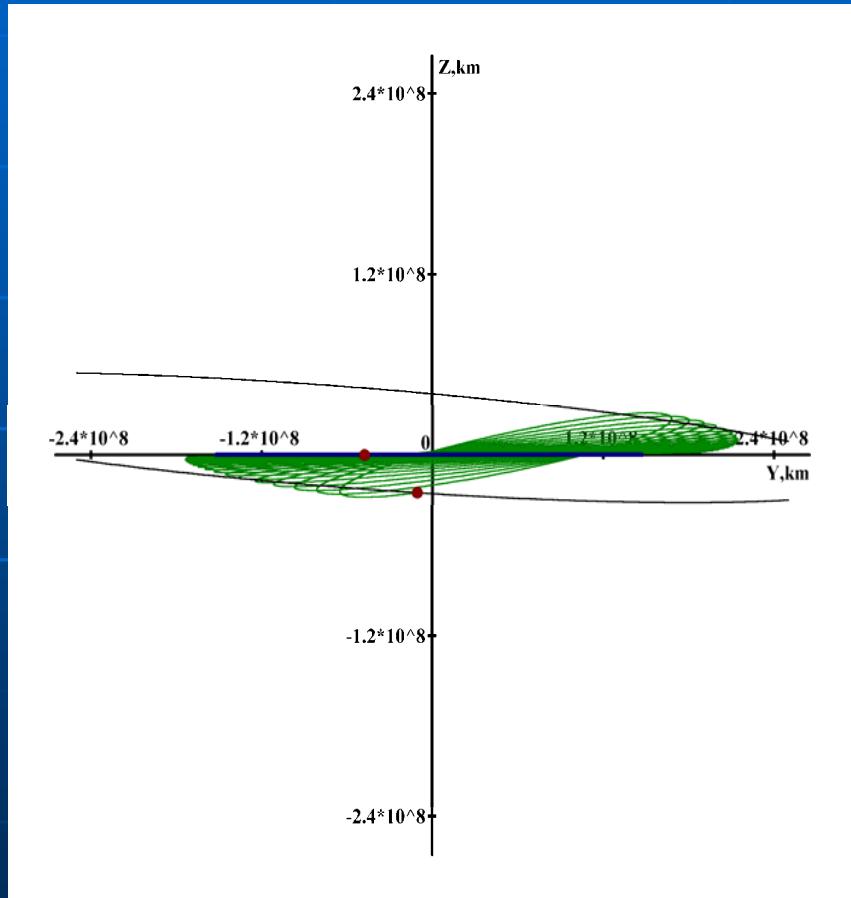
$J=351152$



# Trajectory projection to Sxz - plane



# Trajectory projection to Syz - plane



# Main publications (in “Cosmic Research”)

- **K.G. Grigoriev, M.P. Zapletin and D.A. Silaev**  
Optimal Insertion of a Spacecraft from the Lunar Surface into a Circular Orbit of a Moon Satellite, 1991, vol. 29, no. 5.
- **K.G. Grigoriev, E.V. Zapletina and M.P. Zapletin**  
Optimum Spatial Flights of a Spacecraft between the Surface of the Moon and Orbit of Its Artificial Satellite, 1993, vol. 31, No. 5.
- **K.G. Grigoriev and I.S. Grigoriev**  
Optimal Trajectories of Flights of a Spacecraft with Jet Engine of High Limited Thrust between an Orbits of Artificial Earth Satellites and Moon, 1994, vol. 31, No. 6.
- **K.G. Grigoriev and M.P. Zapletin**  
Vertical Start in Optimization Problems of Rocket Dynamics , 1997, vol. 35, no. 4.
- **K.G. Grigoriev and I.S. Grigoriev**  
Solving Optimization Problems for the Flight Trajectories of a Spacecraft with a High-Thrust Jet Engine in Pulse Formulation for an Arbitrary Gravitational Field in a Vacuum, 2002, vol. 40, No. 1.
- **K.G. Grigoriev and I.S. Grigoriev**  
Conditions of the Maximum Principle in the Problem of Optimal Control over an Aggregate of Dynamic Systems and Their Application to Solution of the Problems of Optimal Control of Spacecraft Motion, 2003, vol. 41, No. 3.